Two-dimensional model for accumulation of pore pressure in marine sediments

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ABSTRACT

A two-dimensional 2-D porous model was developed to investigate the accumulation of pore pressure in marine sediments, in which the volume-averaged Reynolds-averaged Navier-Stokes (VARANS) equations were used as the governing equations for the wave motion and Biot's consolidation theory was used for the porous seabed. Unlike most of the previous investigations on the accumulation of pore pressure in which the amplitude of the shear stress over the wave period was used in the source term, in this study, the source term was re-defined as a time-dependent function using the phase-resolved oscillatory shear stresses. Overall good agreement of both oscillatory and residual pore pressures with previous analytical solutions and experimental data demonstrated the reliability of the model for the prediction of wave-induced pore pressure accumulation. For the case with progressive wave loadings, the liquefaction zone related to the initial incident of the wave phases was formed as a 2-D pattern during the first liquefaction wave period. This 2-D pattern became one-dimensional after one wave period, decreasing progressively, to a constant value after a number of wave cycles. For the case with standing wave loadings, a 2-D liquefaction zone occurs first in the region where the shear strains are highest. Eventually, this 2-D pattern becomes continuous, which implies that even the soil in the anti-node section can be liquefied. Compared with the seabed response under linear wave loading, the pore pressure more easily accumulates to a higher value under non-linear wave loading because of the higher peak in the shear strains. Parametric studies indicate that,

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both the wave characteristics and soil properties affect the maximum relative liquefaction depth (z_L/h) significantly. In general, the maximum liquefaction depth increases as the wave height and as the wave length increase and in shallow water within the seabed, which has a lower permeability and lower relative density.

Keywords: wave-induced seabed response; residual liquefaction; phase-resolved instant shear stress; porous seabed; VARANS equations; Biot's theory.

INTRODUCTION

Wave-induced seabed instability has become an increasingly important issue in the design of foundations around offshore infrastructures. Two mechanisms for wave-induced liquefaction have been reported in previous laboratory studies (Zen and Yamazaki 1990), depending upon how the excess pore pressure is generated. One is transient (or oscillatory) liquefaction, which is usually associated with unsaturated marine soils. It is momentary liquefaction that occurs in the seabed under wave troughs when the encapsulated air dissipates the pressure causing a sharp upwardly directed pressure gradient. The other mechanism is normally seen in fully saturated soils. It is a result of the build-up of excess pore pressure caused by the volumetric compaction caused by the action of cyclic wave loading. In this study, we will focus on the residual liquefaction from the second mechanism.

Numerous laboratory experiments (Tzang 1998; Sumer et al. 1999; Sumer et al. 2012; Sumer 2014) have reported the wave-induced pore pressure build-up mechanism and the existence of residual liquefaction. Based on wave flume tests (Sumer et al. 1999; Sumer et al. 2012), three primary factors have been identified that affect the accumulation of pore pressure, i.e., the cyclic shear stress ratio (τ/σ'_0), the period of cyclic loading, and the number of loading cycles required to reach residual liquefaction. Seed and Rahman (1978) developed a simple one-dimensional (1D) finite element model for earthquake-induced liquefaction to describe the buildup of pore pressure under progressive waves. This model has been further extended analytically and numerically to examine wave-induced residual soil response. McDougal et al. (1989) has investigated a set of analytical solutions for wave-induced pore pressure buildup in a

uniform soil layer. Cheng et al. (2001) proposed an analytical solution to re-examine the solution developed by McDougal et al., noting that the small error of shear stress can lead to a large error in the accumulated pore pressure. Sumer and Fredsøe (2002) has developed an analytical solution using Fourier transforms to evaluate the buildup of pore pressure, based on Biot's consolidation equations. Jeng et al. (2007) re-examined the wave-induced residual soil response by developing both an analytical approximation and a numerical solution, thereby providing a better prediction than the previous solutions (McDougal et al. 1989; Cheng et al. 2001). It is noted that the Sumer and Fredsøe (2002) and the Jeng et al. (2007) models are identical, but with different forms and approaches.

Standing waves often occurs in front of an impervious vertical wall or on the ocean side of composite breakwaters, which are formed by the combination of the reflected waves meeting the incoming waves. Compared with previous investigations for progressive wave-induced liquefaction, studies on the standing wave-induced seabed liquefaction have been relatively rare. One of the leading studies for standing wave induced seabed liquefaction was performed by Sekiguchi et al. (1995), in which the derived a closed-form solution considering 1D poro-elastoplasticity under standing waves. Sassa and Sekiguchi (2001) presented a 2-D elastoplastic constitutive model in a finite element analysis of wave-induced liquefaction in sand beds, comparing the numerical solutions with experimental measurements conducted in a centrifuge wave tank (Sassa and Sekiguchi 1999). Their study showed that the rotation of the principal stress axes in the sand was important in the prediction of wave-induced residual soil response under progressive wave loads. Overall, their results were esatisfactory, except for the maximum residual pore pressure in the soil at the antinodal section. Their experiments showed that the soil can liquefy at the antinodal section; however, the opposite behavior was predicted by their numerical results. Recently, Kirca et al. (2013) presented the results of an experimental study of the seabed residual liquefaction under standing wave loads. This is one of a few available in the literature for standing wave-induced pore pressures.

In all the aforementioned studies, except Sassa and Sekiguchi (2001), for wave-induced

residual pore pressures in marine sediments, the source term was considered as a time-independent function with the maximum amplitude of the oscillatory shear stress. Therefore, the oscillatory and residual mechanisms were not coupled, although they affect each other. In this study, we define the source term as a time-dependent function with the phase-resolved oscillatory shear stress and derive the boundary value problem in 2-D. The numerical results from the present model are verified using the previous analytical solution and the experimental data first. Then, the effect of the nonlinear wave components on the accumulation of the wave-induced pore pressure investigated. Finally, the process of the development of the liquefaction zone and the effect of the wave characteristics and the soil properties on the wave-induced maximum liquefaction depth is suggested.

THEORETICAL FORMULATIONS

The phenomenon of ocean waves propagating over a porous seabed is shown in Figure 1. It is assumed that any deformations of the porous seabed are not large and therefore do not affect the wave-seabed interactions. Non-linear waves are simulated by the previous wave model, and the residual mechanism of the seabed response is modeled by a poro-elastic model. Both wave and seabed models are integrated into a single model.

Wave model

The flow of the incompressible fluid is described by the based on the volume-averaged Reynolds averaged Navier-Stokes (VARANS) equations (Lin and Liu 1999) for the mass conservation and momentum conservation as follows:

$$\frac{\partial \langle \bar{u}_{fi} \rangle}{\partial x_i} = 0, \quad (1)$$

$$\begin{aligned} \frac{\partial \langle \bar{u}_{fi} \rangle}{\partial t} + \frac{\partial \langle \bar{u}_{fj} \rangle}{n(1+c_A)} \frac{\partial \langle \bar{u}_{fi} \rangle}{\partial x_j} = \frac{1}{1+c_A} \left[-\frac{n}{\rho_f} \frac{\partial \langle \bar{p} \rangle^f}{\partial x_i} \right. \\ \left. - \frac{\partial \langle \bar{u}'_{fi} \bar{u}'_{fj} \rangle}{\partial x_j} + \frac{1}{\rho_f} \frac{\partial \langle \bar{\tau}_{fij} \rangle}{\partial x_j} + ng_i \right] - \frac{\langle \bar{u}_{fi} \rangle}{1+c_A} \left[\frac{\alpha'_f (1-n)^2}{n^2 d_{50}^2} \right. \\ \left. + \frac{\beta_f (1-n)}{n^2 d_{50}} \sqrt{\langle \bar{u}_{f1} \rangle^2 + \langle \bar{u}_{f2} \rangle^2} \right] \end{aligned} \quad (2)$$

where u_{fi} is the flow velocity, x_i are the Cartesian coordinates, t is the time, ρ_f is the density of water, p is the pressure, g_i is gravitational acceleration, n and d_{50} are the porosity and equivalent mean diameter of the porous material, respectively, c_A is the added mass coefficient, calculated by $c_A = 0.34(1-n)n$, $\alpha'_f = 200$ and $\beta_f = 1.1$ are empirical coefficients associated with the linear and nonlinear drag force, respectively, and τ_{fij} is the viscous stress tensor of the mean flow, which can be defined as follows:

$$\tau_{fij} = \nu_f \left(\frac{\partial \bar{u}_{fi}}{\partial x_j} + \frac{\partial \bar{u}_{fj}}{\partial x_i} \right) \quad (3)$$

where ν_f is the molecular viscosity. The over-bar represents the ensemble average in the case of waves and the prime denotes turbulent fluctuations induced by the ensemble mean. Note that because the VARANS equations are also valid for steady or uncyclic unsteady flow scenarios, in this case, the over-bar denotes time averaging rather than ensemble averaging. The symbols $\langle \rangle$ and $\langle \rangle^f$ stand for Darcy's volume averaging operator and the intrinsic averaging operator, respectively, and are defined as follows:

$$\langle a \rangle = \frac{1}{V} \int_{V_f} a dv, \quad \text{and} \quad \langle a \rangle^f = \frac{1}{V_f} \int_{V_f} a dv \quad (4)$$

where V is the total averaging volume, and V_f is the portion of V that is occupied by the fluid. The relationship between Darcy's volume averaging operator and intrinsic volume averaging

111 is $\langle a \rangle = n \langle a \rangle^f$. The turbulent kinetic energy (k) and the turbulent dissipation rate (ϵ_f) can be
 112 determined from the k - ϵ_f equations as follows:

$$\begin{aligned} \frac{\partial \langle k \rangle}{\partial t} + \frac{\partial \langle \bar{u}_{fj} \rangle}{n} \frac{\partial \langle k \rangle}{\partial x_j} + \frac{\partial \langle \bar{u}_{fj} \rangle}{n} \frac{\partial \langle k \rangle}{\partial x_j} = & - \frac{\langle \bar{u}'_{fi} \bar{u}'_{fj} \rangle}{n} \frac{\partial \langle \bar{u}_{fi} \rangle}{\partial x_j} \\ & + \frac{\partial}{\partial x_j} \left[\left(\frac{\partial \langle \nu_{et} \rangle}{\sigma_k} + \nu_e \right) \frac{\partial k}{\partial x_j} \right] - \langle \epsilon_f \rangle + n \epsilon_{f\infty} \end{aligned} \quad (5)$$

113

$$\begin{aligned} \frac{\partial \langle \epsilon_f \rangle}{\partial t} + \frac{\partial \langle \bar{u}_{fj} \rangle}{n} \frac{\partial \langle \epsilon_f \rangle}{\partial x_j} = & \frac{\partial}{\partial x_j} \left[\left(\frac{\partial \langle \nu_{et} \rangle}{\sigma_\epsilon} + \nu_e \right) \frac{\partial \epsilon_f}{\partial x_j} \right] \\ & - C_{1\epsilon} \frac{\langle \epsilon \rangle}{n \langle k \rangle} \langle \bar{u}'_{fi} \bar{u}'_{fj} \rangle \frac{\partial \langle \bar{u}_{fj} \rangle}{\partial x_j} - C_{2\epsilon} \frac{\langle \epsilon_f \rangle^2}{\langle k \rangle} + n C_{2\epsilon} \frac{\epsilon_{f\infty}^2}{k_\infty} \end{aligned} \quad (6)$$

114 where ν_{et} is the eddy viscosity and ν_e is the dynamic viscosity, which can be expressed as ν_f/ρ_f .
 115 The empirical coefficients $C_{1\epsilon}$, $C_{2\epsilon}$, σ_ϵ and σ_k are 1.44, 1.92, 1.3 and 1.0, respectively, and are
 116 estimated from stationary flow experiments (Rodi 1980). The $\epsilon_{f\infty}$ and k_∞ are defined as follows:

$$\epsilon_{f\infty} = 39.0 \frac{(1-n)^{2.5}}{n} \left(\langle \bar{u}_1 \rangle^2 + \langle \bar{u}_2 \rangle^2 \right)^{1.5} \frac{1}{d_{50}} \quad (7)$$

$$k_\infty = 3.7 \frac{1-n}{\sqrt{n}} \left(\langle \bar{u}_1 \rangle^2 + \langle \bar{u}_2 \rangle^2 \right) \quad (8)$$

117 Appropriate boundary conditions are required to solve the wave field. With respect to the
 118 mean flow field, the no-slip boundary condition is imposed on the seafloor surface ($u_{fi}=0$).
 119 Neglecting the effect of air flow, the zero-stress condition is adopted on the mean free surface,
 120 ($\tau_{fij} = 0$). For the turbulence field, the log-law distribution of mean tangential velocity in the
 121 turbulent boundary layer is imposed near the rigid boundary. Both the turbulent kinetic energy
 122 (k) and its dissipation rate (ϵ_f) on the free surface are implemented with zero gradient boundary
 123 conditions, (i.e., $\frac{\partial k}{\partial n} = \frac{\partial \epsilon_f}{\partial n} = 0$, in which n is the unit normal on the free surface). The damping zone
 124 is located at two vertical boundaries which are far from the region concerned. More detailed
 125 implementations on the boundary conditions for the wave model are discussed by Lin and Liu
 126 (1999).

Based on the poro-elastic theory by Biot (1941), the governing equations for the force equilibrium in the soil can be written as follows:

$$G\nabla^2 u_s + \frac{G}{1-2\mu_s} \frac{\partial}{\partial x} \left(\frac{\partial u_s}{\partial x} + \frac{\partial w_s}{\partial z} \right) = \frac{\partial p_s}{\partial x}, \quad (9)$$

$$G\nabla^2 w_s + \frac{G}{1-2\mu_s} \frac{\partial}{\partial z} \left(\frac{\partial u_s}{\partial x} + \frac{\partial w_s}{\partial z} \right) = \frac{\partial p_s}{\partial z}, \quad (10)$$

where (u_s, w_s) are the soil displacements in the x - and z -directions, respectively; p_s is the pore pressure; μ_s is Poisson's ratio; and G is the shear modulus of the soil.

The wave-induced soil response consists of two components, a transient (oscillatory) component and a residual (build-up) component. The total soil response can thus be expressed as follows:

$$b = \tilde{b} + \bar{b}, \quad \text{where } \bar{b} = \frac{1}{T} \int b dt \quad (11)$$

where T is the wave period, b denotes the the wave-induced soil response variables (including soil displacements, stresses and pore pressures), $\tilde{b}$ represents the oscillatory component, and $\bar{b}$ represents the residual component. In the following sections, both components will be considered.

138 *Oscillatory soil response*

In this study, a saturated porous seabed is assumed to be hydraulically isotropic with the same permeability K in all directions. With these assumptions, the conservation of mass of pore fluid yields the following:

$$\nabla^2 \tilde{p} - \frac{\gamma_w n_s \beta_s}{K} \frac{\partial \tilde{p}_s}{\partial t} = \frac{\gamma_w}{K} \frac{\partial}{\partial t} \left(\frac{\partial \tilde{u}_s}{\partial x} + \frac{\partial \tilde{w}_s}{\partial z} \right), \quad (12)$$

where $\tilde{p}$ is the wave-induced oscillatory pore pressure, n_x is the soil porosity, γ_w is the unit weight of water in the pore, and β_s is the compressibility of the pore fluid, which is defined as

144 follows:

$$\beta_s = \frac{1}{K_w} + \frac{1-S}{P_{w0}} \quad (13)$$

145 where K_w is the true modulus of elasticity of water (taken as 2×10^9 N/m²), P_{w0} is the absolute
146 water pressure, and S is the degree of saturation.

147 The wave-induced oscillatory soil response is obtained by solving equations (9), (10) and
148 (12) with the appropriate boundary conditions. At the seabed surface ($z = 0$), the boundary
149 conditions are as follows:

$$\tilde{p}_s(x, 0; t) = P_b(x, t), \quad \tilde{\tau}_s(x, 0; t) = \tau_f(x, t), \quad \tilde{\sigma}'_{sz} = 0, \quad (14)$$

150 where p_b is the dynamic wave pressure and τ_f is the wave-induced bottom shear stresses at the
151 seabed surface.

152 At impermeable seabed bottom ($z = -h$), the boundary conditions are expressed as follows:

$$\frac{\partial \tilde{p}_s}{\partial z} = 0 = \tilde{u}_s = 0 = \tilde{w}_s. \quad (15)$$

153 *Residual soil response: Existing 1-D model*

154 By adopting the mechanism of wave-induced residual pore pressure accumulation proposed
155 by Seed and Rahman (Seed and Rahman 1978), several analytical approximations and numer-
156 ical models have been developed (Sumer and Fredsøe 2002; Jeng 2013). All of them are one-
157 dimensional 1-D models based on empirical data of pore pressure accumulation and apply to
158 elastic soil behavior using the following governing equation:

$$\frac{\partial \bar{p}_s^*}{\partial t} = c_v^* \frac{\partial^2 \bar{p}_s^*}{\partial z^2} + f^*, \quad (16)$$

159 where $\bar{p}_s^*$ denotes the wave-induced residual pore pressure using a 1-D model and c_v^* is the

160 coefficient of consolidation, which is defined as follows:

$$c_v^* = \frac{GK}{\gamma_w} \frac{2(1-\mu)}{(1-2\mu) + (2-2\mu)nG\beta_s}. \quad (17)$$

161 In equation (16), the source term (f^*) is expressed as follows (Seed and Rahman 1978;
162 Sumer and Fredsøe 2002; Jeng 2013):

$$f^* = \frac{\partial u_g}{\partial t} = \frac{\sigma'_0}{T} \left[\frac{|\tilde{\tau}_{max}|}{\alpha_r \sigma'_0} \right]^{-\frac{1}{\beta_r}}, \quad (18)$$

163 where u_g is the generation of pore pressure (Seed and Rahman 1978), $|\tilde{\tau}_{max}|$ is the maximum
164 amplitude of the oscillatory shear stress, obtained from the solution of the Biot equations (Hsu
165 and Jeng 1994), and α_r and β_r are obtained by the large-scale simple shear test data correspond-
166 ing to the relative density (D_r) of the soil as proposed by de Alba et al. (1976). The relative
167 density, D_r , is defined as follows:

$$D_r = \frac{e_{max} - e}{e_{max} - e_{min}}, \quad (19)$$

168 where e is the void ratio, and e_{max} and e_{min} are the maximum and minimum void ratios, re-
169 spectively. The coefficients α_r and β_r in equation (18) are defined from the following empirical
170 expressions (Sumer et al. 2012):

$$\alpha_r = 0.34D_r + 0.084, \quad \beta_r = 0.37D_r - 0.46. \quad (20)$$

171 The quantity σ'_0 in equation (18) is the initial effective stress and is expressed as follows:

$$\sigma'_0 = \frac{1 + 2K_0}{3} \gamma' z, \quad (21)$$

172 where K_0 is the coefficient of lateral earth pressure, and γ' is the submerged specific weight of
173 the soil.

174 The above 1-D model for the wave-induced residual pore pressure can be solved with the

175 initial boundary condition, $\bar{p}_s^*(z, 0) = 0$ (Sumer and Fredsøe 2002; Jeng 2013).

176 *Residual soil response: New 2-D model*

177 In this study, the above 1-D model is re-derived to create a two-dimensional (2-D) as fol-
178 lows:

$$\frac{\partial \bar{p}}{\partial t} = c_v \left(\frac{\partial^2 \bar{p}}{\partial x^2} + \frac{\partial^2 \bar{p}}{\partial z^2} \right) + f(x, z, t). \quad (22)$$

179 where c_v is the coefficient of consolidation based on the plain-strain, which is defined as follows:

$$c_v = \frac{GK}{\gamma_w(1 - 2\mu)}. \quad (23)$$

180 The source term ($f(x, z, t)$) for the new model is defined as follows:

$$f(t) = \frac{\partial u_g}{\partial t} = \frac{\sigma'_0}{T} \left[\frac{|\tilde{\tau}_{ins}(x, z, t)|}{\alpha_r \sigma'_0} \right]^{-\frac{1}{\beta_r}}, \quad (24)$$

181 where $\tilde{\tau}_{ins}(x, z, t)$ is the phase-resolved oscillatory shear stress.

182 To solve the 2-D governing equation (22) with the new source term, appropriate boundary
183 conditions are applied, i.e., (a) at the seabed surface ($z = 0$), the residual pore pressure is
184 assumed to be zero ($\bar{p}=0$); (b) at the bottom of the porous seabed with finite thickness ($z = -h$),
185 $\frac{\partial \bar{p}_s}{\partial z} = 0$ at $z = -h$); and (c) lateral boundary conditions are assumed to be zero flux. The seabed
186 model is developed using the COMSOL Multiphysics environment (COMSOL 2010) with the
187 dynamic wave pressures obtained from the wave model (COBRAS).

188 This model reflects the effects of instant oscillatory shear stresses on the pore pressure build-
189 up, which will become a time-dependent function, However, the present model doesn't consid-
190 ers the effects of residual pore pressures on the evolutions of oscillatory shear stresses and shear
191 strains. This is the limitation of the model.

Integration of wave and seabed models

The flow field, including the non-linear water elevation, the velocity field and the wave pressures, are determined from COBRAS. Then we extract the wave pressure along seabed surface from the wave model. This wave pressure is imposed as the boundary condition at the seabed surface of the seabed model. The oscillatory seabed response, including pore water pressure, soil displacement and effective shear stress, is found by solving the Biot consolidation equations using a finite element method. The oscillatory shear stresses are included in the source term and the residual soil response are determined using equation (22).

COBRAS, used as the wave model, has the ability to predict non-linear waves propagating over a sloping seabed (including tsunamis and breaking waves) and the interactions between waves and marine structures, such as breakwaters and pipelines. Even though we only present the results for the case of progressive waves and standing waves, the VARANS model (COBRAS) is integrated with the seabed model such that the entire model. This study is part of the long-term development of the numerical model for fluid-soil-structure interactions, in which the structures will be included in the next project.

RESULTS AND DISCUSSION

Validation of the present model

To validate the present model, we performed the following comparisons between the present model and the previous analytical solutions and experimental data.

- Comparison with 1-D laboratory experiments (Liu and Jeng 2013) for the oscillatory pore pressure under progressive waves.
- Comparison with wave flume tests (Sumer et al. 2012) for residual pore pressure under progressive waves.
- Comparison with wave flume tests (Tsai and Lee 1995) for oscillatory pore pressure under standing waves.

- Comparison with wave flume tests (Kirca et al. 2013) for residual pore pressure under standing waves.

In the first validation, we compare the results of our oscillatory pore pressure with the previous analytical solutions (Hsu and Jeng 1994) and laboratory experiments (Liu and Jeng 2013). Based on Biot's poro-elastic theory, Hsu and Jeng (1994) analytically investigated the wave-induced soil response in an isotropic seabed of finite thickness. This analytical solution has been widely used for the validation of wave-induced oscillatory pore pressure in a porous seabed without structures in the literature (Sumer and Fredsøe 2002). Recently, Liu and Jeng (2013) conducted a series of 1-D laboratory experiments to investigate the vertical profile of pore pressure distributions in marine sediments. The 1-D facility used for their experiments was set up with a vertical cylinder, a 1.8 m soil layer and 0.2 m of water above the deposit. This set up is an improvement on the one originally designed by Zen and Yamazaki (1990). Unlike Zen and Yamazaki (1990), an additional static load was applied on the dynamic load. This allows the facility to simulate the case of large waves, better simulating the natural ocean environment (Liu and Jeng 2013). The numerical results for the maximum vertical oscillatory pore pressure ($\tilde{p}/p_0$) versus relative soil depth (z/h) are shown in Figure 2. As shown in the figure, the present model agrees overall with both the analytical solution and the experimental data. In the comparison, we also include the comparisons between the present model and previous analytical solution for effective normal stresses and shear stresses. Overall, the present model also agrees with the previous analytical solution (Hsu and Jeng 1994).

Sumer et al. (2012) conducted an experimental study for the pore pressure accumulation and liquefaction in marine soils under progressive waves. The experimental data reported in Sumer et al. (2012) are used here to further verify the residual component of the present numerical model. Both the numerical results from the "2-D instant model", the "2-D maximum model" and the 1-D analytical solutions developed by Sumer et al. (2012), are included in this comparison. Note that, the model in which the maximum shear stress over the wave period in the source term are used to simulate the pore pressure accumulation is called the "2-D maximum model".

244 The maximum shear stress in the “2-D maximum model” is actually a 1-D shear stress because
 245 it is independent of the x - direction, similar to the previous research (Sumer and Fredsøe 2002;
 246 Jeng 2013). The model in which the phase-resolved oscillatory shear stress is used as the source
 247 of pore pressure accumulation is called the “2-D instant model”. The input data are tabulated
 248 in Table 1 and the numerical comparisons are presented in Figure 3. As shown in the figure,
 249 there are not significant differences for the wave-induced pore pressure accumulation between
 250 the “2-D maximum model” and the 1D model (Sumer et al. 2012). For the case in which the
 251 phase-resolved shear stresses over the wave period are used as the source of pore pressure ac-
 252 cumulation (“2-D instant model”), the residual pore pressures are relatively small during the
 253 entire build-up process. However, the overall trend of the residual pore pressure of the present
 254 “2-D instant model” captures the experimental data well. This comparison validates our model
 255 and demonstrates the significant improvement of the prediction of the wave-induced residual
 256 pore pressures in marine sediments with the new definition of the source term applied in our
 257 2-D model.

258 In the third comparison, we compare the present results with the previous wave flume tests
 259 (Tsai and Lee 1995) for standing wave-induced oscillatory pore pressures in a porous seabed.
 260 In the experiments, the wave period (T) = 1.5 sec, the wave height (H) = 5.1 cm, the water
 261 depth (d) = 0.45 m, the soil permeability (K) = 1.2×10^{-4} m/s, the porosity (n_e) = 0.38, the
 262 shear modulus (G) = 2.64×10^7 N/m², the seabed thickness (h) = 0.5 m, Poisson’s ratio (μ_s) =
 263 0.29, and the degree of saturation (S) = 0.98. As shown in Figure 4, overall the predictions of
 264 the model agree well with the experimental data.

265 In the fourth validation, we compared the model with the recent experimental data (Kirca
 266 et al. 2013) for the standing wave-induced residual pore pressure. The soil conditions for the
 267 experiments were the same as the second validation (Sumer et al. 2012) and the wave period (T)
 268 = 1.09 s, the wave height (H) = 10.2 cm and the water depth (d) = 0.3 m. As shown in Figure
 269 5, overall the model catches the trend of the experimental data for the standing wave-induced
 270 residual pore pressures.

In Kirca et al. (2013) experiments, the soil pit was divided into two by sealed additional plate. However, in the present numerical model, the configuration of the soil is slightly different from the experiments. This is the reason why the prediction of pore pressures by the model can only catch the trend, compared with the experimental results. Furthermore, in the model, the wave reflection was generated by a vertical wall placed at the end of the computing domain. Furthermore, the vertical wall was extended downward into the seabed. This doesn't allow the pressure flux go through.

Note that the above validations are based on works available in the literature. To the authors' best knowledge, the experiments conducted by Kirca et al. (2013) was the only one provided synchronized time series of residual pore pressure measured at different location in the x -direction. This model further confirms with their experimental results (Kirca et al. 2013)

Effect of nonlinear component of wave loading

The flow field in most of the previous studies (Sumer and Fredsøe 2002; Jeng 2013) are limited to analytical linear progressive wave solutions. In real ocean environments, ocean waves, especially in the shallow water zone, are always characterized as non-linear. Therefore, it is necessary to examine the effect of the nonlinear component of the wave loading in the seabed response, including both the oscillatory pore pressure and the residual pore pressure. With the input parameters shown in Table 2, the distributions of the wave-induced pore pressure under different components of wave loading versus wave cycle are shown in Figure 6(a). The total pore pressure $\tilde{p} + \bar{p}$ (blue lines) and residual pore pressure $\bar{p}$ (red lines) are illustrated in the figure. As shown in the figure, the model simulates the phenomenon of wave-induced residual pore pressure. The model results show that from $t = 0$, when the residual pore pressure is equal to zero, the peak value of the oscillatory pore pressure for a case under a nonlinear wave loading is higher than that for the case under a linear wave loads. This is the reason why the pore pressure for a case under a nonlinear wave loading accumulates. The regions between the two dashed lines in Figures 6(a) and 6(b) were selected for enlargement in Figure 6(c), and a more definite comparison of the residual pore pressure between these two components of wave loads

are shown in Figure 6(d). As shown in the figure, the pore pressure accumulates faster for the case under a nonlinear wave loading.

Liquefaction zone with the present 2-D model

Although residual liquefaction caused by progressive waves has been extensively investigated, studies of standing wave-induced liquefaction are relatively rare. Sassa and Sekiguchi (1999) carried out a series of centrifuge wave tests to investigate seabed liquefaction under standing waves, in which the antinode of the standing wave is formed in the middle of their sediment pit. In this study, the standing waves are obtained in front of an impervious vertical wall by solving the VARANS equations with a finite difference method. The turbulence fluctuations between the wave and the structure are simulated using the volume-averaged $k - \epsilon$ model. The wave parameters are shown in Table 2. In this example, the antinode of the standing wave is formed in the middle of the simulation domain of the integrated model, which is located at $x = 744$ m with wavelength of approximately 112 m. The standing wave is used to analyze of the development of the liquefaction zone and the pore pressure accumulation.

It is well-known that liquefaction occurs when the excess pore pressure reaches the initial effective stress, i.e., $\bar{p}_s = \sigma'_0$. The source term for the residual pore pressure generation is 2-D and time-dependent function in the present model. This feature directly affects the pattern of the liquefaction zone. Using the input data in Table 2, Figure 7(a) shows the resulting variations of wave-induced residual liquefaction zones versus the wave cycle (t/T) for various types of wave loads. As shown in the figure, the liquefaction zone under progressive waves occurs as a 2-D pattern during the first wave period after liquefaction ($t/T = 90$ in this example). The reason there is a 2-D liquefaction zone in the first liquefaction wave period may be from the 2-D phase-resolved shear stress used as the source of the pore pressure. The region where the 2-D pattern occurs is related to the initial incidence of the wave phases. As the progressive wave loading continues, the nature of the liquefaction zone changes from 2-D pattern to 1-D pattern after one wave period. The 1-D pattern travels with the wave and reaches a constant value after several wave cycles.

For the case of the standing waves, as shown in Figure 7(b), the liquefaction zone will occur initially in the region where the shear strains are most significant, then this liquefied zone extends laterally and vertically. Finally even the soil at the antinode section will be liquefied after certain wave cycles. This phenomenon coincides well with what has been discussed by Sassa and Sekiguchi (2001).

In addition to the development of liquefaction zone, it is necessary to investigate the residual pore pressure along x -direction with the present model. The distributions of residual pore pressure along x -direction at three typical locations under different types of wave loads estimated by the 2-D model are presented in Figures 7(c) & 7(d). The model results show that, there are only minor differences in the pore pressure accumulation along x -direction under the effect of progressive waves. Because the liquefaction occurs at $t/T = 90$ in this example, a more definitive comparison of pore pressure accumulation along the x -direction between $t/T = 80$ and $t/T = 100$ is shown in Figure 7(e). The results show that the pore pressure in the soil during the initial 2-D liquefaction pattern, i.e., at $(x, z) = (710, -0.5)$ & $(x, z) = (770, -0.5)$, accumulates faster compared with that at location $(x, z) = (740, -0.5)$. This phenomenon is likely because the difference between the residual pore pressure along x -direction under progressive waves may be related to the difference of the shear strains along the x -direction induced by the initial incidence of the wave phase. After which, every x section will experience the same progressive wave loading as the wave progresses; therefore, after a long loading time, the difference in pore pressure during the first wave cycle can be neglected. However, a strong x -dependence is observed for the case of the standing waves, where the pore pressure can accumulate to a much larger value in the location where the wave-induced shear strains are the highest, compared with the shear strain in the antinode section.

Progressive liquefaction

Sassa et al. (2001) developed an elasto-plastic constitutive model for the wave-induced liquefaction in sand beds with infinite thickness in which the source term was related to the rate of plastic volumetric deformation $\partial \epsilon^p / \partial t$, while the stress ratio τ / σ'_{z0} was still estimated

by the poro-elastic solutions considering the presence of liquefaction front. The maximum liquefaction depth (z_L) increases as time increases, approaching a constant. This behavior is similar to the behavior of the more sophisticated model previously developed for progressive liquefaction (Sassa et al. 2001). The comparison of the distribution of maximum liquefaction depths (z_L) versus time (t) between Sassa's model (Sassa et al. 2001) and the present 2-D instant model are presented in Figure 8. The input data for this comparison are shown in Table 3. The results in Figure 8 show that the maximum liquefaction depth gradually increases and approaches a constant with sufficient time. Although there is a difference in the growth trends between Sassa's model and the present model, the final liquefaction depth predicted by the present instant model matches fairly well with the results predicted by Sassa's elasto-plastic model (Sassa et al. 2001). The stress axes rotation are neglected in the present poro-elastic model as a first approximation, which have been proven to be particularly important in the evaluation of the wave-induced residual liquefaction (Sassa and Sekiguchi 2001). This example is only used to demonstrate that the present 2-D model is capable in the first-hand prediction of the development of progressive liquefaction. For a detailed investigation, the reader still need to refer to Sassa et al. (2001) model.

Effects of the wave characteristics on the progression of the liquefaction depth

It is well-known that wave characteristics play an important role in the evaluation of the wave-induced seabed response (Jeng 2013). Among these, the water depth, the wave period and the wave height are three key wave parameters considered in the present study. Figure 9(a) illustrates the effect of the wave height on the progression of the liquefaction depth in time. As shown in the figure, the maximum liquefaction depth increases faster and accumulate to a larger value under larger wave loadings.

In general, a decrease in water depth (d) results in a decrease in the wave length (L). When the wave height (H) is the same, a decrease in the wavelength will result in a large wave steepness (H/L) and hence a wave that is closer to breaking, i.e., the large wave condition. Therefore, a decrease of the value (d) from 20 m to 18 m causes the final liquefaction depth to more than

halve, as shown by the data in Figure 9(b).

Basically, wave length increases as the wave period increases. The shear strains from the pressure also increase as the wave length increases. As a result, the pore pressure should accumulate to a large value. However, wave flume tests have shown (Sumer et al. 1999; Sumer et al. 2012) that the pore pressure accumulation is not only related to the shear stress ratio ($\tau\sigma'_z$), but also to the period of the cyclic loadings. Therefore, the effect of the wave period on the wave-induced pore pressure accumulation is also examined. As shown in Figure 9(c), the liquefaction depth accumulates more readily in the case with a small wave period. This occurs because the pore pressure and the energy have less time to drain out in the short wave period.

Based on the results presented in Figure 9, it can be concluded that the liquefaction depth increases more easily to accumulate under conditions of: (1) larger amplitude waves, (2) small wave periods and (3) shallow water.

Effects of the soil properties on the progression of the liquefaction depth

In addition to the wave parameters, soil properties are also important for the wave-induced pore pressure in marine sediments (Sumer and Fredsøe 2002; Jeng 2013). The buildup empirical coefficient α_r and β_r are related to the relative density (D_r), while the dissipation rate of the pore pressure are related to the soil permeability (K). Thus, we further examined the effects of K (soil permeability) and D_r (relative density) on the build-up pattern. The seabed characteristics are Poisson's ratio $\mu = 0.35$, the degree of saturation $S_r = 1$, and the seabed porosity $n = 0.425$. Figures 9(d) and 9(e) illustrates the time histories of the progression of the liquefaction depth in the soil with different permeability (K) and relative density (D_r). As shown in Figures 9(d) and 9(e), soils with a low permeability and low relative density increase liquefaction deeper because a high permeability results in a high dissipation rate, which makes the pore pressure more difficult to accumulate. In addition, a decrease in the value of D_r from 0.4 to 0.3 will cause the final liquefaction depth to more than halve, and less time for the soil with a higher permeability to reach its final liquefaction depth.

CONCLUSIONS

In this study, with the source term is defined as 2-D and time-dependent function, a new 2-D model for pore pressure accumulation in marine sediment is proposed. The following conclusions are based on the numerical results:

1. Both the oscillatory component and the residual mechanism are validated against experimental data (Sumer et al. 2012; Liu and Jeng 2013). The comparison indicates that the present “2-D instant model” is reliable for the prediction of the wave-induced residual pore pressures in marine sediments with the new definition of the source term.
2. The residual pore pressure in the soil under nonlinear components of wave loads is more likely to accumulate to a large value compared with that under linear wave loads, because the magnitude of wave-induced shear strains for the case under nonlinear components of wave loads is larger than that under linear wave loads.
3. In the wave field numerical modelling, standing waves were obtained in front of a impermeable seawall, in which the turbulence fluctuations induced by the wave-structure interaction are simulated using the volume-averaged $k - \epsilon$ model. The antinode of the standing wave in the integrated model is formed in the middle of the simulation domain.
4. For the case of progressive wave loads, the liquefaction zone occurs as 2-D pattern during the first liquefaction wave period ($t/T = 90$ in the example). The region of this initial 2-D liquefaction zone is related to the initial incidence of the wave phase. The 2-D pattern changes from 2-D to 1-D in one wave period. This 1-D pattern travels progressively with the wave, and reach a constant value after several wave cycles. For the case of standing wave loads, a 2-D liquefaction zone will occur first in the region where the shear strains are highest. The 2-D zone then expands laterally and vertically to neighbouring points. The soil in the antinode section will eventually undergoing liquefies.
5. There is no significant difference in the pore pressure accumulation in the x - direction for the case under progressive wave loads. However, there is a strong x - dependence in

pore pressure accumulation for the case of standing wave loads. It takes a much longer time for the soil in the antinode section to liquefy compared to the soil in other sections.

6. It is found that there is significant difference of the progress of liquefaction depth versus time between the present model and Sassa's model (Sassa et al. 2001); however, the final liquefaction depths are nearly the same. This indicates that our present 2-D elastic model is able to predict the maximum progressive liquefaction depth. Parametric studies indicate that, the seabed with lower permeability and relative density under a higher energy wave with a short wave period (i.e., larger wave, short wave period, shallow water) is more likely to be liquefied.

Note that this paper presented a new 2-D model for the wave-induced accumulation of pore pressures in marine sediment. This model can be further applied to other cases with marine infrastructures such as offshore pipelines (Zhao et al. 2014).

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TABLE 1. Soil properties and wave characteristics used in the validations.

Seabed characteristics	Value
Soil porosity (n_e)	0.51
Poisson's ratio (μ)	0.29
Shear modulus (G)	1.92×10^6 (N/m ²)
Soil permeability (K)	1.5×10^{-5} (m/s)
Coefficient of lateral earth pressure (K_0)	0.42
Submerged specific weight of soil (γ')	8.14 (kN/m ³)
Degree of saturation (S)	1
Relative density (D_r)	0.28
Thickness (h)	0.4 (m)
Wave characteristics	Value
Wave period (T)	1.6 (s)
Wave height (H)	0.18 (m)
Water depth (d)	0.55 (m)

TABLE 2. Input data for numerical examples.

Seabed characteristics	Value
Soil porosity (n_e)	0.425
Poisson's ratio (μ)	0.35
Shear modulus (G)	5×10^6 (N/m ²)
Soil permeability (K)	10^{-4} (m/s)
Coefficient of lateral earth pressure (K_0)	0.41
Submerged specific weight of soil (γ')	10.73 (kN/m ³)
Degree of saturation (S)	1
Relative density (D_r)	0.2
Thickness (h)	50 (m)
Wave characteristics	Value
Wave period (T)	10 (s)
Wave height (H)	5 (m)
Water depth (d)	16 (m)

TABLE 3. Soil and wave characteristics for verification with Sassa's model.

Seabed characteristics	Value
Soil porosity (n_e)	0.425
Poisson's ratio (μ)	0.35
Shear modulus (G)	5×10^6 (N/m ²)
Soil permeability (K)	1.5×10^{-4} (m/s)
Coefficient of lateral earth pressure (K_0)	0.41
Submerged specific weight of soil (γ')	10.73 (kN/m ³)
Degree of saturation (S)	1
Relative density (D_r)	0.27
Wave characteristics	Value
Wave period (T)	10 (s)
Wave height (H)	6.5 (m)
Water depth (d)	20 (m)

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FIG. 1. Sketch of wave-seabed interaction.

FIG. 2. Vertical distribution of maximum wave-induced oscillatory pore pressure versus relative soil depth for comparison between the present 2-D model (solid lines) with the 1-D experimental results (symbols, Liu and Jeng (2013)) and the analytical solution (dashed lines, Hsu and Jeng (1994)).

FIG. 3. Comparison of the experimental data (Sumer et al., 2012) and the present model results: (a) time histories of the residual pore pressure and (b) vertical distributions of $\bar{p}_s$ for different times.

FIG. 4. The comparison of the standing wave induced oscillatory pore pressure at the nine points in the sand bed between the experimental data (Tsai and Lee, 1995) and the numerical results.

(a) $(x,z)=(0.585,-0.07)$ m

(b) $(x,z)=(0.585,-0.135)$ m

FIG. 5. Comparison of the experimental data (Kirca et al., 2013) and the present model results for the case with standing waves.

FIG. 6. Distribution of the wave-induced pore pressure versus the wave cycle (t/T) under different types of wave loads: (a) Linear wave loads; (b) Nonlinear wave loads; (c) Enlarge comparison; and (d) Comparison of residual pore pressure. $(x,z)=(750,-2)$ m.

(a) Progressive waves

(b) Standing waves

(c) Progressive waves

(d) Standing waves

(e) Enlarge of part (c)

FIG. 7. The histories of the development of the liquefaction zone and pore pressure accumulations along the x -direction under different types of waves (a) and (b) : liquefaction zones at different times; (c) and (d) : pore pressure build up at three points; and (e) enlarged section of part (c)

FIG. 8. Comparison of the progression of the wave-induced liquefaction zone versus time between Sassa's model and the present model.

(a) wave height

(d) relative density (D_r)

(b) water depth

(e) permeability (K)

(c) wave period

FIG. 9. Parametric studies for progress of wave-induced liquefied zone versus time for various (a)–(c) wave and (d)–(e) soil characteristics.