Spectral Analysis of Microarray Gene Expression Time Series Data of *Plasmodium Falciparum*

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Abstract: We propose a new strategy to analyze the periodicity of gene expression profiles using singular spectrum analysis (SSA) and autoregressive (AR) model based spectral estimation. By combining the advantages of SSA and AR modeling, more periodic genes are extracted in the Plasmodium falciparum dataset compared with the classical Fourier analysis technique. We are able to identify more gene targets for new drug discovery, and by checking against the seven well known malaria vaccine candidates, we have found 5 additional genes that warrant further biological verification.

Keywords: Singular spectrum analysis (SSA), autoregressive (AR) model, microarray time series analysis, gene target, Plasmodium falciparum

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1. Introduction

The protozoan parasite Plasmodium falciparum is one of the four Plasmodium species that can cause human malaria, for which there is no effective vaccine yet. The disease is a major killer in many developing countries. In 2002, a complete genome sequence of P. falciparum was reported (Gardner et al., 2002) [3]. The database provides valuable information for researchers to find potentially unique or at least substantially different genes in P. falciparum compared with other species. These genes may be useful in designing drugs that can cause less risk of negative side effects.

Certain genes are expressed only at specific stages of the cell cycle, for example, the intraerythrocytic developmental cycle (IDC). These genes consequently exhibit a periodic pattern of expression. The identification of periodically expressed genes is important for understanding the biochemical functions and gene regulations of P. falciparum. Bozdech et al. have applied the Fourier transform to analyze the periodicity of transcriptome of IDC and offered a detailed description of the four major morphological stages, namely, ring/early trophozoite, trophozoite/early schizont, schizont and early ring (Bozdech et al., 2003) [1]. Their paper revealed that a majority of expression profiles of transcriptome of the IDC showed a high periodicity. The spectral information can be used for further data analysis, such as clustering (Bozdech et al., 2003; Spellman et al., 1998; Le Roch et al., 2003; Rajarajeswari et al., 2005) [1,13,6,11]. Liew et al. have studied the problem of missing data and uneven sampling for the dataset (Liew et al., 2007) [7]. However, the Fourier transform is well known to have limited frequency resolution for short signal analysis due to the so-called windowing or data truncation effect. As discussed below, there are only 46 time points in the gene expression profiles in the IDC data of P. falciparum. This kind of time series would be considered extremely short in signal processing. Furthermore, microarray data usually contain a high level of noise, which can degrade the performance of data analysis algorithms. Thus, effective methods are needed to process noisy and short gene expression time series data.

In this paper, we propose a new scheme for analyzing the periodicity of the transcriptome of the IDC by combining singular spectrum analysis (SSA) and autoregressive (AR) modeling. By using the SSA, the dominant trend can be extracted from the noisy expression profiles and the effect of noise can be reduced effectively. The method described here is an extension of our work presented at CompLife'06 (Du et al., 2006) [2]. Utilizing the advantage of AR modeling in spectral analysis, we are able to analyze the periodicities of the data more accurately. The combination of SSA and AR methods can identify about 90% of genes in P. falciparum and thus gain an advantage over the Fourier analysis in cyclic gene identification.

2 Methods

2.1 Dataset and data preprocessing

The microarray dataset used in this paper is downloaded from http://malaria.ucsf.edu. It contains the expression profiles of 5080 oligonucleotides measured at 46 time points spanning 48 hours during the IDC with one hour time resolution for the HB3 strain. A logarithm transform was applied to the expression ratio of channel Cy5 to channel Cy3.
The mean of each expression profile was subtracted from each profile so that the average log ratio value over the time span is equal to zero.

2.2 Trend estimation of expression profiles using the SSA

Gene expression data generally contain high level of noise. Although spectral analysis can be applied directly to the original data, noise would degrade the results. A preprocessing step should be applied to the original data to reduce the effect of noise before performing spectral analysis.

Singular spectrum analysis (SSA) has been proven to be a powerful tool for processing many types of time series in geophysics, economics, biology, medicine and other sciences (Golyandina et al., 2001) [4], which may have nonlinear characteristics. The main idea of SSA is to extract the underlying trend from short and noisy time series (Vautard et al., 1992) [15]. There is no need to fit an assumed model to the time series since SSA is a robust model-free technique. These properties make SSA a useful technique for gene expression data processing. Using SSA, microarray dataset containing the expression profiles of 5080 oligonucleotides is processed to extract their trend curves and remove noise.

SSA performs singular value decomposition (SVD) on the so-called trajectory matrix obtained from the original time series with subsequent reconstruction of the series. The singular values can be grouped into two separate components: trend component and noise component. With the proper selection of singular values, the trend curve that represents the dominant spectral component can be reconstructed from the original expression profile. In fact, the process of SSA can be considered as a process of data fitting.

Let each expression profiles be a time series \{s_1, s_2, \ldots, s_n, \ldots, s_N\}. The SSA can be performed as follows:

1. Construct the trajectory matrix \(X_{M,K}\) from the original series by sliding a window of length \(M\) \((M \leq N/2)\), \(K = N - M + 1\).

\[
X_{M,K} = (x_{ij} = s_{i+j-1}) = \begin{bmatrix}
    s_1 & s_2 & \cdots & s_K \\
    s_2 & s_3 & \cdots & s_{K+1} \\
    \vdots & \vdots & \ddots & \vdots \\
    s_M & s_{M+1} & \cdots & s_N
\end{bmatrix}
\]

2. Perform the SVD of the matrix \(R = XX^T\). The singular values are ranked in decreasing order \(\lambda_1 > \lambda_2 > \cdots > \lambda_M\) and the trajectory matrix is decomposed into a series of components \(X_i\), where \(X_i = \sqrt{\lambda_i} U_i V_i^T\) \((i = 1, 2, \ldots, M)\) are rank-one biorthogonal matrices, the \(U_i\) and \(V_i\) are the left and right singular vectors of the matrix \(X\), respectively.

3. Group a specified number of leading singular values \(\lambda_i\) and sum the corresponding components \(X_i\), then the resultant matrix is \(X'_{M,K} = (x'_{ij})\). The number of singular values to use is discussed below.

4. Reconstruct the data series \(\{s'_1, s'_2, \ldots, s'_n, \ldots, s'_N\}\) by averaging the elements of matrix \(X'\) over the ‘diagonals’ \(i+j=n+1\). The choice \(n = 1\) gives \(s'_{11} = x'_{11}\), for \(n=2\) we have \(s'_{22} = (x'_{12} + x'_{21})/2\) and so on.
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One important consideration in SSA is how to select the singular values to reconstruct the expression profiles. If we plot the singular values, the graph contains an initial steep slope, representing the signal, and a “flat floor”, representing the noise level (Vautard et al., 1989) [14]. The dominant component trend can be reconstructed from the expression profiles using the leading singular values that contain most of the energy. The ratio of the leading singular values and the total eigenvalues is defined as follows:

\[
E = \frac{\sum_{i=1}^{d} \lambda_i}{\sum_{i=1}^{M} \lambda_i}
\]

where \(d\) is the number of leading singular values.

For the majority of transcriptome of IDC, the leading two singular values of expression profiles contain most of the energy and correspond to the signal (Figure 1). Therefore, we group the leading two singular values to reconstruct the expression profiles (Liu et al., 2003) [8]. An example of trend extraction using the SSA is shown in Figure 2.

\[\text{Figure 1} \text{ The singular values of the data matrix for Dihydrofolate Reductase-Thymidylate Synthase (DHFS-TS).}\]
Figure 2 Signal extraction of DHFS-TS using the SSA. The leading two singular values which represent 90% energy are chosen for the reconstruction. The window length is $M = 23$.

2.3 The AR model based spectral estimation

Periodicity in genome-wide gene expression datasets has been widely used to identify cell-cycle-regulated genes. Being a popular technique for time series analysis, power spectrum estimation has often been used for periodicity identification. If the data are highly periodic, the calculated power spectrum would show sharp peaks at the corresponding frequency points. As one of the nonparametric power spectrum estimation methods, the Fourier analysis is relatively simple, and could be readily calculated using the fast Fourier transform (FFT) algorithm. Let the discrete data sequence be $s(n)$, $0 < n < N - 1$, the corresponding estimate of the power density spectrum is

$$
\hat{P}_{ss}(\omega) = T \sum_{l=-(N-1)}^{N-1} \hat{r}_{ss}(l)e^{-j\omega lT}
$$

where $T$ is the sampling interval, $r_{ss}$ and $N$ represent the autocorrelation sequence and the number of data samples of signal $s$, respectively. However, the gene expression data series are often short and noisy, and the spectral resolution from the Fourier-based power spectrum estimation would be seriously degraded due to the well-known windowing effect, which is caused by the unrealistic assumption of nonparametric methods that the autocorrelation estimate $r_{ss}(l)$ is zero for $l > N$.

The AR model for the time series $s(n)$ is given by
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\( s(n) = -\sum_{p=1}^{P} a_p s(n-p) + u(n) \)  \hspace{1cm} (3)

where \( a_p \) are the AR coefficients, \( P \) is the order of the AR model, and \( u(n) \) is a white noise sequence. The forward linear prediction estimation is given by

\( \hat{s}(n) = -\sum_{p=1}^{P} a_p s(n-p) \)  \hspace{1cm} (4)

where \( \hat{s} \) is used to denote an estimate of \( s \). Therefore, the AR model can be interpreted as the estimation at current time index \( n \) based on \( P \) past samples, while \( u(n) \) is the estimation error.

Note that the AR method is a generative method, where the signal generation model is given by Equation (4). Hence, AR modeling can extrapolate the values of the autocorrelation for \( l > N \). The parameter \( P \) is called the order of the AR model and it can be estimated from the correlation matrix of the observed data. The corresponding power spectrum density can be estimated as follows,

\[
P_{ss}(\omega) = T \sum_{l=-\infty}^{\infty} r_{ss}(l) e^{-j\omega lT} = \frac{T\sigma^2}{1 + \sum_{p=1}^{P} a_p e^{-j2\pi pT}}^2
\]  \hspace{1cm} (5)

where \( P_{ss}(\omega) \) represents the power spectral density of the signal \( s \) at frequency \( \omega \).

Equation (5) shows that the region of support of the autocorrelation \( r_{ss} \) is \( (-\infty, \infty) \). For this reason, the AR power spectral density estimators do not possess the sidelobe phenomenon of the classic spectral estimators and can yield higher frequency resolution than nonparametric methods (Marple 1987; Yan 2002; Yan et al., 2007; Yeung et al., 2004) [9,16,17,18]. There are a number of algorithms developed for estimating the parameters \( a_k \). In this work, we adopt the Yule-Walker method to estimate these parameters (Yan 2002; Yeung et al., 2004) [16,18]. The Yule-Walker method, also called the autocorrelation or windowed method, computes the AR parameters by forming a biased estimate of the signal’s autocorrelation function, and solving the least squares minimization of the forward prediction error (Marple 1987) [9].

2.4 The combination of SSA and AR modeling

The major advantage of the AR model based power spectrum over classical Fourier analysis is its high frequency resolution obtained by fitting a relatively high order AR model to the original data sequence. However, the AR spectrum is also sensitive to noise. When the signal to noise ratio is low, the accuracy of the parameter estimation in Equation (3) would be reduced substantially. A higher order AR model has to be used to improve the frequency resolution, but the usage of higher order would induce the appearance of spurious peaks. According to Keppenne and Penland (Keppenne et al.,
SSA can be used as a data-adaptive noise filter. By applying AR power spectrum estimation to the SSA pre-filtered data series, noise-free or noise-reduced frequency spectrum could be obtained. As shown in Figure 3, due to the removal of noise using the SSA, spurious peaks are eliminated from the spectrum. We should point out here that SSA and AR modeling are general signal processing methods and can be applied to the analysis of many types of time series data. There are also software packages available to implement these algorithms. For an example of the software, see http://www.systat.com/.

\[ S = \frac{\text{power}_i}{\text{power}_{\text{total}}} \]  

where $\text{power}_i$ and $\text{power}_{\text{total}}$ represent the power over $f_i$’s ROI and the total power of the signal, respectively.

First, each expression data is reconstructed using SSA. Only the expression profiles with the singular value ratios in Equation (1) ($d = 2$) greater than 0.6 are to be...
reconstructed. Second, the AR spectrum is calculated for each reconstructed expression profiles. Then the frequency $f_i$ at peak value point and the ratio of the power in $f_i$'s ROI to the total power are calculated according to Equation (6). Finally, the profiles are screened according to following rule: if the power ratio calculated previously is larger than 0.7 (which is the same value as that used in Bozdech et al. (2003) [1]), the corresponding profile would be selected as periodic, otherwise, we consider it lacking of periodicity and discard it.

3 Results

3.1 Periodic profile detection

We have tested our algorithm on the expression data of the IDC of P. falciparum. There are a total of 5080 expression profiles in the dataset. In DNA microarray data analysis, one of the major challenges is to dissociate actual gene expression values from noise effectively. We used the SSA for trend estimation and have only selected those profiles whose dominant components contain most of the energy for further analysis. Then we performed spectrum analysis of the reconstructed expression profiles by using AR spectral estimation. When an expression profile is highly periodic, its power spectrum would have sharp peaks at the corresponding frequency points. We utilized the power ratio to filter the reconstructed expression profiles. The histogram of the power ratio of the expression profiles of the IDC data is shown in Figure 4. By using our periodicity detection method, 4496 periodic profiles are found to be periodic. Compared with the Bozdech et al. (2003) [1]’s result, an additional 777 periodic oligonucleotides are detected using our algorithm.
3.2 Analysis of classification result

It is generally accepted that the function of a gene is related to the initial phase of its expression profile (Bozdech et al., 2003; Rustici et al., 2004) [1,12]. So for the convenience of gene function classification, we have ordered the expression profiles of the extracted 4496 oligonucleotides according to their peak time points of expression profiles. Figure 5 shows a continuous cascade of gene expressions, which correspond to the developmental stages throughout the IDC, that is, ring, trophozoite and schizont stages. According to the sharp transitions of ring-to-trophozoite (at the 17h time point), trophozoite-to-schizont (at the 29h time point) and schizont-to-rings stages (at the 45h time point) (Bozdech et al., 2003) [1], 4496 selected genes could be categorized into four stages on the basis of the peak time points of expression profiles in Figure 5. The comparison of the classification results of the oligonucleotides assigned to these stages by our method with those in Bozdech et al. (2003) [1] is shown in Table 1. Bozdech et al. (2003) [1] has listed all possible functional gene of P. falciparum. Among these functional genes, some cannot be detected using the method in Bozdech et al. (2003) [1] due to the low power ratio score. In contrast, our method using the SSA helps to smooth out noise and makes the dominant spectral component much more evident. In addition, the AR spectrum produces higher frequency resolution than classical Fourier spectrum. By combining advantages of SSA and AR models, periodicity in the gene expression profiles is extracted much more accurately. More functional genes are detected compared
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with the Fourier analysis technique used in Bozdech et al. (2003) [1]. In Table 2, we provide the list of functional genes identified by our algorithm that was not found by the method in Bozdech et al. (2003) [1].

![Phaseogram of the transcriptome of the IDC of P. falciparum](image)

**Figure 5** The phaseogram of the transcriptome of the IDC of P. falciparum. 4496 genes are ordered along the y axis in the order of the time of their peak expression

<table>
<thead>
<tr>
<th>Stages</th>
<th>Our method</th>
<th>Method in Bozdech et al. (2003) [1]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ring/early Trophozoite</td>
<td>1970</td>
<td>1563</td>
</tr>
<tr>
<td>Trophozoite/early Schizont</td>
<td>1524</td>
<td>1296</td>
</tr>
<tr>
<td>Schizont</td>
<td>709</td>
<td>625</td>
</tr>
<tr>
<td>Early ring</td>
<td>293</td>
<td>235</td>
</tr>
</tbody>
</table>

**Table 1** Comparison of the classification results of oligonucleotides in three different stages. More genes can be identified using our method

<table>
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</tr>
</tbody>
</table>

**Table 2** The list of genes for different functional groups of P. falciparum detected by our method that was not found by the method in Bozdech et al. (2003) [1]
Genes expressed during the mid to late schizont and early-ring stage encode proteins predominantly involved in highly parasite-specific functions facilitating various steps of host cell invasion. The highly parasite-specific functions implied that they should serve as good targets for both drug discovery and vaccine-based antimalarial strategies (Bozdech et al. 2003) [1]. The additionally identified genes are distributed in the 777 additional oligonucleotides found by our method and they would be useful for the future identification of novel targets for anti-malarial therapies. In general, there are two gene targets to be considered for new drug discovery: apicoplast-targeted genes and proteases. In Table 3, we provide a comparison of the number of the two gene targets detected by our method and by Bozdech et al. (2003) [1].

### Table 3

<table>
<thead>
<tr>
<th>Potential genes targets</th>
<th>Our method</th>
<th>The method in Bozdech et al. (2003)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Apicoplast-targeted</td>
<td>409</td>
<td>358</td>
</tr>
<tr>
<td>proteases</td>
<td>115</td>
<td>88</td>
</tr>
</tbody>
</table>
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Merozoite invasion is one of the most promising target areas for antimalarial vaccine development. Among these invasion proteins are seven of the well known malaria vaccine candidates, including Apical Merozite Antigen-1 (AMA1), Merozoite Surface Protein-1 (MSP1), Merozoite Surface Protein-3 (MSP3), Merozoite Surface Protein-5 (MSP5), Erythrocyte Binding Antigen-175 (EBA175), Rhopty-Associated Protein-1 (RAP1) and Ring-infected Erythrocyte Surface Antigen-1 (RESA1). It is now widely accepted that genes with the same or similar function are likely to have similar expression profiles. Therefore, we have used the similarity to identify genes with possible involvement in the merozoite invasion process. The similarity of 4496 expression profiles to seven known vaccine candidates is evaluated using the Euclidian distance. There are a total of 267 genes, constituting the top 6% of the detected periodic genes in the IDC, with minimum distance to these seven genes (the same distance threshold is adopted from Bozdech et al. (2003) [1]). Five additional genes are detected by our method, which are listed in Table 4. They are all from the late schizont stage.

<table>
<thead>
<tr>
<th>Oligonucleotides</th>
<th>Genes</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>n139_5</td>
<td>PF14_0757</td>
<td>Hypothetical protein</td>
</tr>
<tr>
<td>n143_54</td>
<td>PF14_0183</td>
<td>RNA helicase</td>
</tr>
<tr>
<td>n168_2</td>
<td>PF14_0530</td>
<td>Ferlin, putative</td>
</tr>
<tr>
<td>opfblob0035</td>
<td>PFD0430c</td>
<td>Hypothetical protein</td>
</tr>
<tr>
<td>opfl0111</td>
<td>PFL2110c</td>
<td>Hypothetical protein</td>
</tr>
</tbody>
</table>

4 Conclusion

Spectral analysis of the transcriptome of the asexual intraerythrocytic development cycle (IDC) of P. falciparum offers an effective means for the studies of cyclic gene expression and future drug and vaccine targets. In this paper, we have proposed a new scheme based on SSA and AR power spectral analysis for the detection of periodically expressed genes in the IDC of P. falciparum. SSA allows the dominant trend to be extracted from the noisy expression profiles, and subsequent AR spectrum analysis provides higher frequency resolution in the periodicity detection. We have detected more periodically expressed profiles in the P. falciparum dataset. Compare with the results of Bozdech et al. (2003), we have obtained 14 additional functional genes undetected by them. That is, we have detected more gene targets for new drug discovery, and we have identified 5 additional genes that are potential antimalarial vaccine candidate. The result shows that our method can not only detect more periodic genes but also can find genes that could be useful targets for potential drug/vaccine design.

Acknowledgments

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References

