Dictionary Learning Based Feature Level Domain Adaptation for Cross-scene Hyperspectral Image Classification

Minchao Ye, Yuntao Qian, Member, IEEE, Jun Zhou, Senior Member, IEEE and Yuan Yan Tang, Fellow, IEEE

Abstract

A big challenge in hyperspectral image (HSI) classification is small size of labeled data for classifier learning. In real remote sensing applications, we always face the situation that an HSI scene is not labeled at all or is with very limited number of labeled pixels, but we have sufficient labeled pixels in another HSI scene with similar land cover classes. In this paper, we undertake classification on a target HSI scene containing no labeled sample or only few labeled samples with the help of a similar source HSI scene having relatively large size of labeled samples. We name this classification problem as cross-scene classification. The main challenge of cross-scene classification is spectral shift, i.e., even for the same class in different scenes, their spectral distributions may have significant deviation. As all or most training samples are drawn from the source scene and the prediction is performed on the target scene, the difference in spectral distribution would greatly deteriorate the classification performance. To solve this problem, we propose a dictionary learning based feature level domain adaptation technique, which aligns the spectral distributions between source and target scenes by projecting their spectral features into a shared low-dimensional embedding space by multitask dictionary learning. The basis atoms in the learned dictionary represent the common spectral components, which span a cross-scene feature space to minimize the effect of spectral shift. After the HSIs of two scenes are transformed into the shared space, any traditional HSI classification approaches can be used. In this paper, sparse logistic regression is selected as the classifier. To be more specific, if there are a few labeled pixels in the target domain, multitask sparse logistic regression is used to further promote the classification performance. The experimental results on both synthetic and real HSIs show the advantages of the proposed method for cross-scene classification.

Index Terms

Hyperspectral image, cross-scene classification, domain adaptation, dictionary learning, multitask learning.

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I. INTRODUCTION

Pixel classification is an important application on hyperspectral images (HSI). A challenge in HSI classification is small size of training data, which makes the training models ill-posed. In order to solve this problem, semi-supervised learning and active learning are widely used in HSI classification. Semi-supervised learning makes use of both labeled and unlabeled data to train a classifier, including semisupervised SVM [1], [2], graph-based semisupervised learning [3], manifold-based semisupervised learning [4]. Active learning is an interactive information extraction approach [5]–[7]. During training procedure, it selects informative unlabeled samples and label them, which minimizes the cost of labeling to reach a good classification performance. Both semisupervised learning and active learning approaches assume that the pixels belonging to the same land cover class follow an identical distribution in the feature space.

In real remote sensing applications, we always encounter the situation that an HSI scene (called target scene) to be classified has only very few labeled samples or even not any labeled sample due to high labor costs of labeling or other limitations. On the contrary, other similar scenes (source scenes) may have sufficient labeled samples. In this case, a natural idea is to make use of the class-specific information in source scenes to help target scene classification. we call this problem as cross-scene classification. For example, if a city in somewhere suffered from a natural disaster such as earthquake, flooding, or hurricane, we want to understand the field condition and assess the disaster losses through hyperspectral remote sensing and HSI processing techniques including classification. It is not realistic to obtain many labeled samples in the captured HSIs on this site, but we can easily found some HSIs with more labeled samples captured from similar cities. These cities share a common set of land cover objects. For example, in urban areas there always are roads, buildings, rivers, trees, grasses, et al, while in rural areas there commonly have fields with various crops. The common land cover classes make it possible to transfer knowledge between similar HSI scenes.

The most straightforward method for cross-scene classification is to use the source domain samples directly. When no labeled samples are available in the target scene, the source domain samples can be directly employed to train a classifier. When a few labeled samples are available in the target scene, we can merge the labeled samples in both scenes for training. However this simple way suffers from spectral shift, i.e., pixels belonging to same land cover class may vary in spectral distribution from two different HSI scenes. This phenomenon is also called covariate shift, population drift or dataset shift [4], [8]–[12], which occurs when the training and testing scenes are spatially or temporally different. The spectral shift is caused by many factors, including different atmospheric and light conditions at the image acquisition stage, different sensor nonlinearities, different substance compositions of the same land cover class in different sizes and times, etc. [13]. Therefore, even though a large number of training data are available in the source scenes, the classifiers trained from those data or the combined data from both source and target scenes may perform poorly on the testing samples from the target scene [14], [15]. Therefore, a more complex strategy is necessary to better solve the cross-scene classification problem.

The key issue of cross-scene classification is to reduce the spectral shift in feature level or classifier level by domain adaptation. Classifier level domain adaptation tunes the parameters and structures of a classifier model
during training procedure to make the classifier generalize to target domain. Bruzzone and Prieto [13] proposed a maximum-likelihood (ML) based retraining method to tackle spectral shift in multi-temporal remote sensing images. Firstly, an ML classifier is trained on source scene in a supervised manner, producing the a priori probability and conditional density for each class. Then the statistical distribution of pixels in target scene is represented by a mixed density distribution with as many components as the classes to be recognized. Finally, retraining this ML classifier in target domain becomes a mixture density estimation problem that can be solved by expectation maximization (EM) algorithm. Alternatively, Rajan et al [8] used binary hierarchical classifier (BHC) to solve this problem. The BHC involves recursively decomposing a multiclass ($C$-classes) problem into ($C-1$) binary meta-class problems by building a binary tree. BHC takes similarity among classes into consideration, where similar classes are in the same meta-class (parent node). The structure of BHC tree conveys the relationship between classes, which can be shared between source and target scenes. The BHC transfers the hierarchy of the classes from source scene to target scene and re-trains each binary classifier via EM algorithm. Sun et al [11], [12] applied support vector machine (SVM) with cross-domain kernels for domain adaptation, whose cost function combines two factors simultaneously, one is minimizing the distribution distance between two domains in reproducing kernel Hilbert space, and the other is minimizing the structural risk function of SVM. The classifier level domain adaptation is focused on modifying the classifier while the transformation between source and target domains is not explicitly displayed, therefore, dependence on specific classifier is its main disadvantage.

Feature level domain adaptation attempts to directly adjust the feature space domains of source and target data sets to decrease their discrepancy of distribution, after that any classifier can be used. Tuia et al [16] proposed manifold alignment with graph matching, which assumes that source and target data lie on two different manifolds. Graph matching is used for finding a mapping to align these two manifolds, by which target data can be transformed into the source domain, or vice versa. Thus the classifier trained from source scene can be applied on the target scene. However, finding a precise graph matching is a difficult task, especially with a large difference between source and target scenes in terms of class distribution and spectral distribution.

In this paper, we propose a dictionary learning based feature-level domain adaptation method which projects the spectral feature spaces of source and target scenes into a shared subspace spanned by atoms in the dictionary. In this shared subspace, the spectral shift between two domains is reduced. A multitask joint dictionary learning (MTJDL) scheme is used to extract the common components between target and source scenes. Dictionary learning is to find the intrinsic subspace that can sparsely represent the data in the form of a linear combination of basis atoms. Multitask learning is a powerful learning technique which binds several related learning tasks to improve their performance by a shared model [17]. MTJDL combines the advantages of both dictionary learning and multitask learning, which provides cross-scene feature extraction, domain adaptation, and dimensional reduction at the same time, all of which are critical factors to improve the performance of cross-scene HSI classification. The coding coefficient over the learned dictionary is utilized as cross-scene feature, by which any classifier can be adopted.

The rest of this paper is organized as follows. Section II introduces the basic theory of domain adaptation, especially feature level domain adaptation, and its relation with cross-scene HSI classification. Section III presents MTJDL based domain adaptation for cross-scene feature extraction and the subsequent classification algorithms for
cross-scene HSI classification. Experiments on both synthetic and read-world data sets are reported in Section IV to show the benefit brought by domain adaptation. At the end, conclusions are drawn in Section V.

II. CROSS-SCENE HSI CLASSIFICATION AND DOMAIN ADAPTATION

Due to spectral shift, classical statistical learning algorithms are no longer valid for cross-scene HSI classification as they are always based on the assumption that both training and testing samples are drawn from an identical distribution. To show the shift of spectral distribution between two scenes, we select two spatially distant regions of interest from AVIRIS Indiana HSI image which covers a large area (see Fig. 1), and each region is treated as a scene. The spectral distributions of two classes Soybeans-CleanTill-EW and Corn-CleanTill-EW in two scenes are shown in Fig. 2, from which we can see that the spectral distributions belonging to the same land cover class are different in two scenes. This phenomenon indicates there exists spectral shift between these two scenes.

To mathematically discuss spectral shift, we firstly give some key notations and definitions. In this paper, $X_S$ and $X_T$ represent the spectral feature spaces in source and target domains respectively. $X_S$ and $X_T$ are the samples drawn from source and target domains following the marginal distributions $P(X_S)$ and $P(X_T)$. $y_S$ and $y_T$ are the
corresponding class labels (if available), and the conditional distributions in two domains are denoted by \(P(y_S|X_S)\), \(P(X_S|y_S)\) and \(P(y_T|X_T)\), \(P(X_T|y_T)\), respectively. According to possible scenarios, several kinds of distribution shifts are usually considered, including class imbalance, covariate shift, conditional shift and target shift [18], [19], whose conditions are listed in Table I. For cross-scene HSI classification, target shift of spectral distribution is an ordinary case, i.e., \(P(X_S) \neq P(X_T)\) and \(P(y_S|X_S) \neq P(y_T|X_T)\). Obviously, a classifier learned with the training samples from source domain \((X_S, y_S)\) can not be directly used to classify \(X_T\).

To evaluate the degree of spectral shift, we define two criteria, namely class specified mean signature angle distance (CSMSAD) matrix and spectral shift index (SSI). Signature angle distance (SAD) is a commonly used criterion to calculate the distance between two spectral vectors \(x_1\) and \(x_2\) in HSI, which is defined as

\[
SAD(x_1, x_2) = \arccos \left( \frac{\langle x_1, x_2 \rangle}{\|x_1\| \|x_2\|} \right).
\]

The CSMSAD matrix \(M\) defines the class specified spectral distance between source and target scenes, whose elements are calculated as

\[
m_{pq} = \frac{1}{\#(C_S^{(p)}) \#(C_T^{(q)})} \sum_{\substack{i \in C_S^{(p)}, \ j \in C_T^{(q)}}} SAD((x_S)_i, (x_T)_j)
\]

where \(C_S^{(p)} = \{i|(y_S)_i = p\}\) is a set including pixels belonging to the \(p\)th class in source scene, \(C_T^{(q)} = \{j|(y_T)_j = q\}\) is a set including pixels belonging to the \(q\)th class in target scene, and \(\#(\cdot)\) stands for the size of a set. \(m_{pq}\) indicates averaged spectral distance between the \(p\)th class in source scene and the \(q\)th class in target scene. The diagonal elements in \(M\) have positive correlation with the degree of spectral shift, while the non-diagonal elements in \(M\) have negative correlation with the degree of spectral shift. A large value of \(m_{qq}\) indicates that the spectral distributions of the \(q\)th class in source domain and target domain have large difference, i.e., spectral shift of the \(q\)th class is significant. A small value of \(m_{pq}(p \neq q)\) means that the spectral distribution of the \(p\)th class in source domain is similar to that of the \(q\)th class in target domain, which causes the cross-scene HSI classification to be more difficult. Therefore, we define SSI to measure the degree of spectral shift, which is based on the matrix \(M\).

\[
SSI = \frac{1}{C^2} \sum_{p=1}^{C} \sum_{q=1}^{C} m_{pq}/m_{qq}
\]

The larger the value of SSI, the larger the degree of spectral shift. When there exists a large spectral shift, domain adaptation is necessary.

<table>
<thead>
<tr>
<th>Table I: Different types of distribution shifts</th>
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<tbody>
<tr>
<td><strong>Name</strong></td>
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<tr>
<td>----------</td>
</tr>
<tr>
<td>Class imbalance</td>
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<tr>
<td>Covariate shift</td>
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<td>Conditional shift</td>
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<td>Target shift</td>
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To solve the problem of spectral shift, domain adaptation is one of the main techniques. The aim of domain adaptation is to reduce the distribution shift between two domains by exploiting their underlying correlations or shared representation components and structures. Domain adaptation has been widely applied in cross-domain learning problems, including image classification, handwritten character recognition, text classification [15], [20], [21]. Classifier level and feature level domain adaptations are two principal approaches. Classifier level methods learn a classifier for target domain from pre-learned classifiers for source domains through the correlation between source and target domains. A cross domain SVM can be learned by a convex combination of loss functions of SVMs in source and target domains [22]. Yang et al [23] proposed to learn a “delta function” from the source and target data, and then added it to the SVM model for domain adaptation. Duan et al [24] imposed a data-dependent regularizer of smoothness into least-squares SVM to enforce the target classifier to share similar decision values with the source domain classifiers. Xu and Sun [25] proposed an Adaboost cross domain classifier in which a new parameter was designed to indicate domain relationship, and the combination of multiple learners was adopted to output the target hypothesis. Instance weighted classifiers try to compensate the differences in marginal/conditional distributions between domains by adaptively weighting instances [26]–[29]. Instance weighting can eliminate the negative effect of the misleading instances that are not compatible with target domain [15]. The weights of instances are usually decided by their prediction confidences during co-training procedure.

Feature level method (also called subspace method in some literature) is more direct and general for domain adaptation. It maps the source and target domain spaces into a common feature subspace where the distribution shift is reduced [30]–[33]. Shown by Fig. 3, feature level domain adaptation is to find feature projections $\pi_S(\cdot)$ and $\pi_T(\cdot)$ so that the distributions of projected features $P(\pi_S(X_S))$ and $P(\pi_T(X_T))$ are similar, and the projected feature $\pi_T(X_T)$ is more discriminative [34]. One idea is to represent source and target data on Grassmann manifold, and then use the geodesic path is to obtain intermediate subspaces [30]. Other work adopted kernel method to look for the shared feature representation in a reproducing kernel Hilbert space (RKHS). To this end, Pan et al [35] designed an objective function with two goals, one is minimizing the distance of source and target distributions in the RKHS, and the other is preserving the data variance in each domain.
Another type of feature level domain adaptation is dictionary learning. Dictionary learning on signals and images has attracted tremendous interest in recent years, as signals or images can be more effectively represented in a specific subspace spanned by atoms in a dictionary. In particular, a data-driven dictionary can adapt to input data so its generated new feature space can provide more robust and discriminative data representations for many applications [36]–[38]. In domain adaptation point of view, dictionary learning generates a domain-invariant space which are jointly learned from both source and target data [34]. Dictionary learning based domain adaptation was first used for self-taught learning where the number of labeled training samples is limited but there exist a large amount of unlabeled but related samples. For example, a large amount of unlabeled data can be used to learn a dictionary with K-SVD algorithm, and then the coding coefficients on the dictionary are treated as domain-invariant features [20], [39]. Through this dictionary-based feature representation, classification performance on the target domain can be greatly improved. Ni et al [40] learned an initial dictionary from source data, then the dictionary was gradually updated using target domain information, and finally a dictionary was learned for the target domain. Shekhar et al [41] proposed a robust method for learning a single dictionary to optimally represent both source and target data. In particular, they proved that learning a dictionary on a low-dimensional space reduces the irrelevant information in original features in different domains. Furthermore, the problem of small-training-size in HSI classification goes along with high-dimensionality problem, as HSIs always have hundreds of bands and their transformed feature spaces such as wavelet transformed feature space [42] will have higher dimensions. Therefore, dictionary learning based domain adaptation is a suitable choice for its combination of dimensionality reduction and cross-scene feature extraction. Other properties of this method will be further discussed in the next section.

III. FEATURE LEVEL DOMAIN ADAPTATION FOR CROSS-SCENE HSI CLASSIFICATION

Feature level domain adaptation for cross-scene HSI classification can be divided into two steps, i.e., cross-domain feature extraction and classifier training. The first step is to transform the spectral domains of source and target scenes into a shared feature space in which spectral shift can be reduced by extracting their inherent identical structure. Nonnegative matrix factorization (NMF) based dictionary learning is used in this paper to generate the shared feature space. This method has an intrinsic relation with the mixture spectral model of hyperspectral imaging, so it can give a physical interpretation for this shared feature space. The second step is to learn a classifier in the shared feature space with training samples from source scene or from both source and target scenes. In this paper, sparse logistic regression (SRL) is selected as the classifier. SRL combines classifier learning and feature selection into one frame, which selects discriminative features from the shared feature spaces so that spectral shift can be further reduced.

A. Cross-scene feature extraction via multitask NMF based dictionary learning

A general assumption for unsupervised domain adaptation is that there exist certain discriminative features shared by both domains [30], [43]. From the dictionary learning based domain adaptation point of view, this assumption implies that samples in source and target domains share a common dictionary on which they can be consistently represented. The representation coefficients on the learned dictionary are utilized as the cross-domain features for
the training and testing samples in different scenes. These new features in the common space not only have less distribution shift between source and target scenes, but also have more discriminative ability between different classes. Here, multitask joint dictionary learning (MTJDL) is proposed for learning a shared dictionary from both source and target domains. The model framework is illustrated in Fig. 4, in which the samples from source and target domains are used to train a shared dictionary, and then the coefficient vectors are taken as the new extracted features. During dictionary learning, the class labels of samples are not considered, i.e. both samples with or without labels can be used for dictionary learning, so this method belongs to unsupervised dictionary learning.

There are several unsupervised dictionary learning algorithms such as method of optimized directions (MOD) [44], K-SVD [45], NMF [46], etc. Among them, NMF has some distinct advantages. NMF can learn a parts-based representation of the data by factorizing a nonnegative matrix into two nonnegative factor matrices. One factor matrix can be seen as a dictionary, and the other is the linear representation on this dictionary. From the view of linear spectral mixture model, two factor matrices decomposed by NMF correspond to the endmembers and the abundances, so NMF and its extensions have been successfully used for hyperspectral unmixing [47]–[50]. In this sense, the learned dictionary by NMF also can be seen as a spectral library consisting of the endmembers in the HSIs being processed. In spite of the potential spectral shift between scenes, the spectra of pixels in different scenes can be approximated by linear combination of endmembers, so dictionary learning based domain adaptation for cross-scene HSI classification can be considered as a problem of learning their common spectral library and then using the corresponding abundances as the new features of pixels. Although the conditions of NMF for dictionary learning is weaker than those for unmixing, for example, the number of endmembers (the size of spectral library) is not required to be estimated accurately, the interpretation of domain adaptation from the mixture model point of view is intuitive and beneficial to interpreting dictionary learning based domain adaptation.

For learning a common dictionary from two or more domains, multitask NMF is adopted. Multitask NMF, or
called simultaneous NMF, was first proposed by Badea [51] to extract common gene expression profiles that are shared by colon and pancreatic adenocarcinoma. In the multitask NMF, two or more NMF tasks are bound together by sharing a common factor matrix (i.e., dictionary). When applied to cross-scene HSI data sets, multitask NMF can be considered as a tool to extract a common set of endmembers shared by different but related HSI data sets.

The model of multitask NMF is defined as

\[
\min_{D \in \mathbb{R}^n_{++} \times p} \left\{ \sum_{i=1}^{m_S} \| (x_S)_i - D(v_S)_i \|^2_F + \sum_{j=1}^{m_T} \| (x_T)_j - D(v_T)_j \|^2_F \right\}
\]

\[
\text{s.t. } (v_S)_i \geq 0, \quad i = 1, 2, \ldots, m_S,
\]

\[
(v_T)_j \geq 0, \quad j = 1, 2, \ldots, m_T,
\]

where \((x_S)_i \in \mathbb{R}_{++}^n\) and \((x_T)_j \in \mathbb{R}_{++}^n\) are the spectral profiles of the pixels in source and target domains, respectively. \(D \in \mathbb{R}_{++}^{n \times p}\) is the common dictionary matrix shared between two domains, whose columns are basis atoms. \((v_S)_i\) and \((v_T)_j\) are the coefficient vector of \((x_S)_i\) and \((x_T)_j\), respectively. The dictionary size is set smaller than the number of spectral bands, i.e., \(p < n\), thus a dimensional reduction is embedded in feature extraction, which is beneficial to small-training-size classification.

Following solution for the traditional NMF, multiplicative update (MU) algorithm can be used to solve Eq. (4) by an alternating optimization procedure. Eq. (4) can be briefly written as

\[
F(D, V_S, V_T) = \|X_S - DV_S\|^2_F + \|X_T - DV_T\|^2_F
\]

where \(X_S = [(x_S)_1, (x_S)_2, \ldots, (x_S)_{m_S}]\), \(V_S = [(v_S)_1, (v_S)_2, \ldots, (v_S)_{m_S}]\), \(X_T = [(x_T)_1, (x_T)_2, \ldots, (x_T)_{m_T}]\), and \(V_T = [(v_T)_1, (v_T)_2, \ldots, (v_T)_{m_T}]\). The partial derivatives of \(F\) with respect to \(V_S\), \(V_T\) and \(D\) are calculated as

\[
\frac{\partial F}{\partial V_S} = 2D^T DV_S - 2D^T X_S
\]

\[
\frac{\partial F}{\partial V_T} = 2D^T DV_T - 2D^T X_T
\]

\[
\frac{\partial F}{\partial D} = 2DV_S V_S^T - X_S V_S^T + 2DV_T V_T^T - X_T V_T^T
\]

Using the Karush-Kuhn-Tucker (KKT) conditions, we set \(\frac{\partial F}{\partial V_S} = 0\), \(\frac{\partial F}{\partial V_T} = 0\), \(\frac{\partial F}{\partial D} = 0\), and get the MU rules, i.e.,

\[
V_S \leftarrow V_S \odot (D^T X_S) \odot (D^T DV_S)
\]

\[
V_T \leftarrow V_T \odot (D^T X_T) \odot (D^T DV_T)
\]

\[
D \leftarrow D \odot (X_S V_S^T + X_T V_T^T) \odot (DV_S V_S^T + DV_T V_T^T)
\]

After alternatively updating \(V_S\), \(V_T\) and \(D\), the minimization of objective function Eq. (5) can be achieved. Finally, the extracted high level features \((V_S\) and \(V_T\) are fed into a suitable classifier for training and prediction.
B. Classification algorithm

After cross-scene feature extraction, many classical classifiers can be applied, such as support vector machine (SVM) [52], neural networks [53], sparse representation [54], et al. Here sparse logistic regression (SLR) is used, which selects a small number of important/discriminative input variables such that the output of a system can be approximately predicted. It can reduce the disturbance of noisy and irrelevant variables, increase the modeling accuracy and robustness, and improve the interpretation of the system. Some simple and fast computational algorithms have been proposed to deal with large-scale problem. Various applications in computer vision, data mining, and signal processing have proven its effectiveness [42]. In the case of cross-scene HSI classification, since multitask NMF based dictionary learning is unsupervised, it does not consider the discrimination for different land cover classes. SRL enables us to select discriminative features from the shared feature space for further reducing distribution shift and increasing classification accuracy.

In the training procedure, the following objective function of SLR is minimized,

\[
\min_{w,c} \sum_{i=1}^{m} \log(1 + \exp(-y_i(w^T v_i + c))) + \lambda \|w\|_1
\]  

(12)

where \( v_i \) is the feature vector and \( y_i \in \{1, -1\} \) is the class label of the \( i \)th training sample. The optimization algorithm for (12) can be found in [55], [56]. After the coefficients \((w, c)\) are estimated, the classifier works in a probabilistic way to label the input test sample \( x \) using its feature vector \( v \).

\[
P(y = 1|x) = \frac{1}{1 + \exp(-(w^T v + c))}
\]  

(13)

For multi-class problem, one-versus-one voting scheme can be utilized.

Multitask NMF based unsupervised learning dictionary can reduce spectral shift, but cannot completely clear it. Therefore, even in a shared feature space, the classifiers for source scene and target scene need to have subtle nuances if we want to reach further improved cross-scene classification. When a few labeled samples are available in target scene, we can train two classifiers for source and target scenes respectively, making them not only have consistency but also preserve their distinct identities. As a multitask version of SLR, multitask SLR (MTSLR) is used to simultaneously train two SLR models with the label samples in source and target scenes respectively, but these two SRL models share a common discriminative feature subset while the non-discriminative features and the features incompatible between two domains are discarded [17]. Different from SRL based cross-scene classifier that trains a single SRL model for both source and target scenes, MTSLR provides two strongly related but little differentiated classifiers for two different scenes, which can further reduce impact of the residuary distribution shift after dictionary learning based feature level domain adaptation.

The objective function of MTSLR is defined as

\[
\min_{w_{S,T}, c_{S,T}} \left\{ \sum_{i=1}^{m_S} \log(1 + \exp(-(y_S)_i(w_{S}^T(v_{S})_i + c_S))) + \sum_{j=1}^{m_T} \log(1 + \exp(-(y_T)_j(w_{T}^T(v_{T})_j + c_T))) + \lambda \|w_{S,T}\|_{2,1} \right\}
\]  

(14)
The white elements in $w_S$ and $w_T$ stand for zero elements.

where $(v_S)_i$ and $(v_T)_j$ are the features of training samples in source and target domains obtained by NMF based MTJDL. $(y_S)_i$ and $(y_T)_j \in \{1, -1\}$ are their corresponding class labels. $w_S$ and $w_T$ are sparse coefficient vectors, and $c_S$ and $c_T$ are the corresponding intercept terms. The model framework is shown in Fig. 5 where two SLR models are trained for source and target domains, respectively (see the first and second terms in Eq. (14)). Rather than separately training two SLR models, we bind them by sharing a same sparse structure (or called sparse pattern) in coefficient vectors via $\ell_{2,1}$ regularization (the last term in Eq. (14)), which is defined as

$$
\|\|w_S, w_T\|\|_{2,1} = \sum_{i=1}^{n} \sqrt{(w_S)^2_i + (w_T)^2_i}.
$$

The regularization parameter $\lambda$ controls the sparsity level in $w_S$ and $w_T$. The MTSLR model completes joint feature selection and training of two classifiers at the same time.

Since the $\ell_{2,1}$ norm regularization term in objective function (14) is non-differentiable at certain points, we cannot directly minimize the whole objective function by the basic optimization methods such as gradient descent, etc. One of valid algorithms to solve the non-smooth problem is proximal gradient descent [57]–[59].

We denote the logistic loss functions in source and target domains as

$$
\mathcal{L}_S(w_S, c_S) = \sum_{i=1}^{m_S} \log(1 + \exp(-(y_S)_i (w_S^T v_S)_i + c_S))
$$

$$
\mathcal{L}_T(w_T, c_T) = \sum_{j=1}^{m_T} \log(1 + \exp(-(y_T)_j (w_T^T v_T)_j + c_T))
$$

thus the objective function in Eq. (14) is written as

$$
\mathcal{L}_S(w_S, c_S) + \mathcal{L}_T(w_T, c_T) + \lambda \|\|w_S, w_T\|\|_{2,1}.
$$

Its differentiable part and non-differentiable part are optimized iteratively:
1) apply gradient descent on the differentiable part (i.e., $L_S + L_T$) without considering $\ell_{2,1}$ regularization;
2) apply proximal operator (or called shrinkage in some literatures) for $\ell_{2,1}$ regularization.

The detailed algorithm steps are listed in Algorithm 1. Once $w_T, c_T$ are obtained, an input test sample $x$ in target scene can be classified in the same way as Eq. (13).

**Algorithm 1** Proximal gradient descent for MTSLR

**Input:**
- Input features of training samples from source and target domains $V_S \in \mathbb{R}^{n \times m_S}, V_T \in \mathbb{R}^{n \times m_T}$,
- Corresponding class labels $y_S \in \mathbb{R}^{m_S}, y_T \in \mathbb{R}^{m_T}$,
- Regularization parameter $\lambda$.

**Output:**
- The coefficient vectors for source and target domains $w_S \in \mathbb{R}^n, w_T \in \mathbb{R}^n$ and the corresponding intercepts $c_S \in \mathbb{R}, c_T \in \mathbb{R}$.

1: Initialize $w_S = 0, w_T = 0, c_S = 0, c_T = 0$.
2: repeat
3: Optimize $L_S$ and $L_T$ with gradient descent:

$$
\begin{align*}
    w_S &\leftarrow w_S - \alpha \nabla_{w_S} L_S \\
    c_S &\leftarrow c_S - \alpha \nabla_{c_S} L_S \\
    w_T &\leftarrow w_T - \alpha \nabla_{w_T} L_T \\
    c_T &\leftarrow c_T - \alpha \nabla_{c_T} L_T
\end{align*}
$$
where $\alpha$ is step size obtained by line search.
4: Apply proximal operator to handle $\ell_{2,1}$ regularization:

$$
[w_S, w_T] \leftarrow \operatorname{arg \ min}_W \|W - [w_S, w_T]\|_F^2 + \lambda \|W\|_{2,1}
$$

which can be solved by shrinkage

$$
W[i] = \begin{cases} 
(1 - \frac{\alpha \lambda}{\|U[i]\|_2}) U[i], & \|U[i]\|_2 > \alpha \lambda \\
0, & \text{otherwise}
\end{cases},
$$
where $U = [w_S, w_T]$ and $U[i]$ is $i$th row of $U$.
5: until convergence is reached.
6: return $w_S, w_T, c_S, c_T$. 

IV. EXPERIMENTAL RESULTS

In this section, we will validate the proposed cross-scene HSI classification methods on several synthetic and real-world data sets. According to whether the labeled training samples are available in target scene or not, we divide the comparative experiments into two groups. The first group deals with the case that only labeled samples in source scene are available. Following three algorithms are used:

- **Source domain SLR (SD-SLR):** It trains an SLR model by only using the training samples in the source scene, and then the learned SLR model is directly applied to the testing samples in target scene for prediction. Note that this straightforward scheme does not consider any domain adaptation at all, and therefore is regarded as the baseline when no labeled training sample is available in target scene.

- **Transductive support vector machine (TSVM):** It is a very popular classifier level domain adaptation method, which handles the transductive learning by retraining [26]. At first, a classifier is trained using only the labeled samples in source scene, and then this classifier is applied to the unlabeled samples to determine their labels in target scene. Second, the unlabeled samples are added to the training set with the assigned labels to update the classifier. Afterwards, several retraining steps are performed in iterations, and each iteration includes reassigning the class labels of unlabeled samples in target scene and retraining the SVM.

- **SD-MTJDL-SLR:** It is the proposed algorithm in the paper, which learns a shared dictionary by the samples (labeled and unlabeled) in both source and target scenes using multitask NMF based MTJDL model, and then trains an SLR classifier and classifies all testing samples in the new and shared space. As no labeled samples are validate in target scene, the training of SRL only uses the labeled samples in source scene, which is the same as SD-SLR, but the spectral shift in the shared space is less than that in the original spectral space.

The other group cope with the setting that there are a relative large amount of labeled samples in source scene and a small number of labeled samples in target scene. Following five algorithms are taken into experimental comparison:

- **Target domain SLR (TD-SLR):** It only uses the labeled training samples in target scene to train an SLR model in the original spectral feature space, and then it is applied to the testing samples in target scene. This method does not use any information of the source scene, so it is seen as the baseline in the case that the labeled training samples exist in target scene.

- **Merge-SLR:** It merges all labeled training samples within both source and target scenes into a united training set, then an SLR model is trained with this training set in the original spectral feature space for classification. It does not consider spectral shift between source and target scenes, i.e., domain adaptation is not used.

- **TD-MTJDL-SLR:** Like TD-SLR, it also only use the labeled training samples in target scene, but the feature extraction is based on MTJDL. It firstly uses multitask NMF to learn a shared dictionary with labeled and unlabeled samples in both source and target scene, and then trains an SLR classifier on this space with just the labeled samples in target scene.

- **Merge-MTJDL-SLR:** It is our proposed method in the paper. The only difference with TD-MTJDL-SLR is that Merge-MTJDL-SL uses both training samples in source and target scenes.
The spectral signatures for generating the synthetic data

<table>
<thead>
<tr>
<th>Source</th>
<th>Target</th>
</tr>
</thead>
<tbody>
<tr>
<td>(\mathbf{x}_1^\text{s} = \text{Douglas-Fir YNP-DF-1})</td>
<td>(\mathbf{x}_1^\text{t} = \text{Douglas-Fir YNP-DF-2})</td>
</tr>
<tr>
<td>(\mathbf{x}_2^\text{s} = \text{Espruce-Sfir YNP-SF-2})</td>
<td>(\mathbf{x}_2^\text{t} = \text{Espruce-Sfir YNP-SF-3})</td>
</tr>
<tr>
<td>(\mathbf{x}_3^\text{s} = \text{Grass-Fescue-Whiteat YNP-FW-1})</td>
<td>(\mathbf{x}_3^\text{t} = \text{Grass-Fescue-Whiteat YNP-FW-2})</td>
</tr>
<tr>
<td>(\mathbf{x}_4^\text{s} = \text{Lodgepole-Pine YNP-LP0-MOD})</td>
<td>(\mathbf{x}_4^\text{t} = \text{Lodgepole-Pine YNP-LP0-VIG})</td>
</tr>
<tr>
<td>(\mathbf{x}_5^\text{s} = \text{Lodgepole-Pine YNP-LP1-A})</td>
<td>(\mathbf{x}_5^\text{t} = \text{Lodgepole-Pine YNP-LP1-B})</td>
</tr>
</tbody>
</table>

- **MTJDL-MTSLR**: It is proposed in the paper to further improve feature level domain adaptation by training two SRL models for source and target scenes respectively in a structured constraint. Compared with Merge-MTJDL-SLR, MTJDL-MTSLR not only reduces spectral shift with unsupervised dictionary learning, but also considers the residual spectral shift in a supervised classifier learning procedure.

The main reason of selecting the above methods for experiments is to find: 1) the impact of spectral shift on cross-scene HSI classification; 2) the usefulness of source information to target scene classification; 3) the effect of the proposed domain adaptation methods.

Model parameter setting is a critical factor to ensure fair comparisons. For SD-SLR, TD-SLR and Merge-SLR, we test their SRL model with parameter \(\lambda \in \{10^{-1}, 10^{-2}, 10^{-3}, \ldots, 10^{-7}\}\), and select the value of parameter with the highest classification accuracy for comparison. For TSVM, similar to the default settings of SVM\(^{\text{light}}\), the parameter \(C\) is adaptively estimated [60]. Two parameters of SD-MTJDL-SLR, TD-MTJDL-SLR and MTJDL-MTSLR are set as \(p \in \{5, 6, \ldots, 30\}\), and \(\lambda \in \{10^{-1}, 10^{-2}, \ldots, 10^{-7}\}\). In the comparison, we select the best parameter values by cross-validation.

### A. Experiments on synthetic data

To give a quantitative analysis on synthetic data, we generate the synthetic data from the USGS digital spectral library [61]. Several factors are taken into consideration for preferably simulating the real situation of cross-scene HSI classification: 1) There is spectral shift between source and target scenes, i.e., \(P(\mathbf{x}_s^t) \neq P(\mathbf{x}_t^t)\) and \(P(y_s|\mathbf{x}_s^t) \neq P(y_t|\mathbf{x}_t^t)\). 2) There is similarity of spectral distribution for the same class between source and target scenes, i.e., the same land cover class consists of the same or similar materials and the corresponding distributions in different scenes. 3) There exists discrimination of spectral distributions between different classes in both of source and target scenes. To ensure the difficulty of cross-scene classification, the separability between different classes is not set high.

With these considerations, we generate the synthetic data by linear spectral mixture model:
• We select twenty spectral profiles from the USGS library, which are categorized into four groups, and each contains five spectral profiles of five materials (or called endmembers in linear spectral mixture model). These four groups are used to separately generate two classes within two scenes, i.e., “Source Class 1”, “Source Class 2”, “Target Class 1”, “Target Class 2”.

• For each class, we use similar endmembers for source and target scenes to ensure that a land cover class consists of similar materials, e.g., \((x^S_1)_1 = \text{Douglas-Fir YNP-DF-1}\) is very similar to \((x^T_1)_1 = \text{Douglas-Fir YNP-DF-2}\), which are both sub-categories of Douglas-Fir.

• Each class is generated by linear combination of five endmembers in the corresponding group, e.g., a sample of class 1 in source domain can be generated by \(x^S_1 = \sum_{i=1}^{5} (\alpha^S_1)_i (x^S_i)_1\) (see Table II)

• The abundances of each sample in a class is generated randomly by Gaussian distribution. To make reasonable spectral shift between source and target domains, the distribution of abundances vary between source and target scenes (see Table II), e.g. \((\alpha^S_1)_1 \sim \mathcal{N}(0.1, 0.05^2)\) and \((\alpha^T_1)_1 \sim \mathcal{N}(0.3, 0.05^2)\) have different mean values.

• To make the classification more challenging, we use a band subset containing 40 bands (bands 41–80 from the original data), which decreases the discrimination between classes.

In summary, the spectral shift in the synthetic data is rooted in the different but similar endmembers and the different abundances when generating different samples of a class in source and target domains. Spectral profiles of some randomly selected samples are plotted in Fig. 6.

In experiments on synthetic data, the number of source domain training samples is set to 500 per class (thus 1000 in total). In the experiments where labeled training samples are available in target domain, we select 5 samples per class (thus 10 in total). Whether training samples are available in target domain or not, 1000 testing samples per class are drawn from target domain to evaluate the classification performance. In the following experiments, overall accuracy (OA), average accuracy (AA) and kappa coefficient (\(\kappa\)) are utilized as performance criteria. Note that since two classes have the same number of test samples, OA = AA always holds for synthetic data.

Firstly, we discuss the relationship between model parameters and classification accuracy. For multitask NMF
based dictionary learning, the dictionary size $p$ is an important parameter. For SLR and MTSLR, there is only one parameter $\lambda$ which controls the sparsity level. Therefore, Fig. 7 shows that the classification accuracy changes with different values of $p$ and $\lambda$ for SD-MTJDL-SLR, TD-MTJDL-SLR, Merge-MTJDL-SLR and MTJDL-MTSLR methods, where the range of $p$ is from 5 to 30, and $\lambda$ from $10^{-7}$ to $10^{-1}$. The red point represents the parameter setting that archives the best OA.

It is found that a dictionary with small size ($p$) can better reduce spectral shift, which is consistent with the conclusion made in [41]. Although the best values of $\lambda$ are very different for these four methods, it can also be seen that $\lambda$ should be set to a small value to reach a high accuracy. Methods on how to determine the degree of sparsity have been proposed in the literature, which are beyond the scope of our paper.

Then we give the comparative classification results in Table III, where the first three rows correspond to the case that the training samples in target domain is not available, while the last five rows are under the condition that both a limited number of training samples and a relative large amount of training ones are available in target and source domains, respectively. Their CSMSAD matrix along with the confusion matrices of classification are illustrated in Fig. 8. In the case when no training sample exists in target domain, SD-SLR classifies all the testing samples in
TABLE III  
CLASSIFICATION ACCURACY ON SYNTHETIC DATA

<table>
<thead>
<tr>
<th>Training sample Source</th>
<th>Algorithm</th>
<th>OA (AA)</th>
<th>(\kappa)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1000 0</td>
<td>SD-SLR</td>
<td>0.5045</td>
<td>0.0090</td>
</tr>
<tr>
<td>1000 0</td>
<td>TSVM</td>
<td>0.4840</td>
<td>-0.0320</td>
</tr>
<tr>
<td>1000 0</td>
<td>SD-MTJDL-SLR</td>
<td>0.7970</td>
<td>0.5940</td>
</tr>
<tr>
<td>0 10</td>
<td>TD-SLR</td>
<td>0.8860</td>
<td>0.7720</td>
</tr>
<tr>
<td>0 10</td>
<td>TD-MTJDL-SLR</td>
<td>0.8990</td>
<td>0.7980</td>
</tr>
<tr>
<td>1000 10</td>
<td>Merge-SLR</td>
<td>0.5005</td>
<td>0.0010</td>
</tr>
<tr>
<td>1000 10</td>
<td>Merge-MTJDL-SLR</td>
<td>0.8115</td>
<td>0.6230</td>
</tr>
<tr>
<td>1000 10</td>
<td>MTJDL-MTSLR</td>
<td>0.9695</td>
<td>0.9390</td>
</tr>
</tbody>
</table>

the target domain Class 1 (see Fig. 8(b)), resulting in a very poor OA/AA of 0.5045. This indicates that directly training a classifier in source domain and applying it to target domain is not a good choice due to spectral shift. For TSVM, though knowledge transfer is considered, more testing samples are misclassified (see Fig. 8(c)), i.e., its classification accuracy is even worse than SD-SLR. This is caused by the overlapped sample distribution between “Source Class 2” and “Target Class 1” (see Fig. 6). Compared with SD-SLR and TSVM, SD-MTJDL-SLR has a much higher classification accuracy, which is also illustrated in Fig. 8(d). This indicates the proposed MTJDL based domain adaptation can greatly reduce spectral shift and improve the cross-scene classification performance.

When some training samples in target domain are also available, the situation becomes to be more complicated. Both TD-SLR and Merge-SLR are based on the original spectral features, the former only uses the target domain training samples, and the latter uses all training samples in two domains. It can be obviously seen that TD-SLR is much better than Merge-SLR, i.e., the training samples in source domain play a negative effort. It again indicates that spectral shift make a classifier directly learned from just source domain or both source and target domains is not valid to target domain classification. Their corresponding versions in the shared feature space, TD-MTJDL-SLR and TD-MTJDL-SLR, also reflect the same fact in the experiments, but the classification accuracies of TD-MTJDL-SLR and TD-MTJDL-SLR are higher than those of TD-SLR and Merge-SLR respectively, especially the improvement of TD-MTJDL-SLR is very significant when compared with TD-SLR. This is a further evidence that the proposed feature level domain adaptation is useful to reduce spectral shift, but it also indicates that spectral shift is not totally cleared. Our MTJDL-MTSLR method not only considers their consistency in the shared spare, but their difference (remained distribution shift) as well, so it achieve the best classification performance.

B. Experiments on real-world data

Now we turn to the real-world cross-scene HSI classification. Three cross-scene HSI datasets are used, including Indiana scenes, Pavia scenes and Shanghai-Hanghzou scenes.

The whole Indiana scene was captured by AVIRIS sensor on June 12, 1992 during a flight over 25 × 6 mile portion of Northwest Tippecanoe County, Indiana [62]. The size of the original whole HSI data is 614 × 2166 × 220,
where the last dimension is the number of bands. Band 120 of the original whole scene is displayed in Fig. 1. We select two spatial disjointed subsets (the regions in the red boxes) as source and target scenes, respectively. Both source and target scenes are sized $400 \times 300 \times 220$. We select seven land cover classes shared by both scenes for classification, which are listed in Table IV. The data cubes and corresponding ground truth maps of two sub-scenes are illustrated in Fig. 9.

In the experiments on Indiana data, the number of source domain training samples is set to 180 per class (thus 1260 in total). The number of target domain training samples is set to 20 per class (thus 140 in total) in the case when the training samples are available in target scene. The remaining labeled samples in target scene are used as testing samples to evaluate the classification performance. All experiments are conducted in the same way as

![Fig. 8. CSMSAD matrix and confusion matrices of synthetic data. (a) CSMSAD matrix. (b) confusion matrix of SD-SLR. (c) confusion matrix of TSVM. (d) confusion matrix of SD-MTJDL-SLR. (e) confusion matrix of TD-SLR. (f) confusion matrix of TD-MTJDL-SLR (g) confusion matrix of Merge-SLR. (h) confusion matrix of Merge-MTJDL-SLR. (i) confusion matrix of MTJDL-MTSLR.](image-url)
TABLE IV
NUMBER OF LABELED SAMPLES IN EACH LAND COVER CLASS WITHIN INDIANA SCENES

<table>
<thead>
<tr>
<th>Class</th>
<th>Labeled samples</th>
<th>Source scene</th>
<th>Target scene</th>
</tr>
</thead>
<tbody>
<tr>
<td>#</td>
<td>Name</td>
<td></td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>Concrete/Asphalt</td>
<td>4867</td>
<td>2942</td>
</tr>
<tr>
<td>2</td>
<td>Corn-CleanTill</td>
<td>9822</td>
<td>6029</td>
</tr>
<tr>
<td>3</td>
<td>Corn-CleanTill-EW</td>
<td>11414</td>
<td>7999</td>
</tr>
<tr>
<td>4</td>
<td>Orchard</td>
<td>5106</td>
<td>1562</td>
</tr>
<tr>
<td>5</td>
<td>Soybeans-CleanTill</td>
<td>4731</td>
<td>4792</td>
</tr>
<tr>
<td>6</td>
<td>Soybeans-CleanTill-EW</td>
<td>2996</td>
<td>1638</td>
</tr>
<tr>
<td>7</td>
<td>Wheat</td>
<td>3223</td>
<td>10739</td>
</tr>
</tbody>
</table>

Fig. 9. Source and target scenes in Indiana datasets. The upper row is the source scene, while the lower row is the target scene. (a) Data cubes. (b) Ground truth maps.

in synthetic data. The accuracies obtained from different algorithms are listed in Table V. The CSMSAD matrix and their confusion matrices are shown in Fig. 10. Like the results on the synthetic data, the results on Indiana data also demonstrate that the proposed multitask NMF based dictionary learning is a good choice for feature level domain adaptation, and MTSLR can further reduce the impact of distribution shift after domain adaptation. SD-MTJDL-SLR and MTJDL-MTSLR achieve the highest accuracies respectively when the training samples in target are available or not. It should be noted that the effect of domain adaptation is different for different classes, which is due to the complicated relation between classes in spectral distribution. For example, comparing Fig. 10(d) with Fig. 10(b), we find that SD-MTJDL-SLR greatly improves the classification accuracy of class 3, but it fails
TABLE V
CLASSIFICATION ACCURACY ON INDIANA DATA

<table>
<thead>
<tr>
<th>Training sample Source</th>
<th>Target</th>
<th>Algorithm</th>
<th>OA</th>
<th>AA</th>
<th>κ</th>
</tr>
</thead>
<tbody>
<tr>
<td>1260</td>
<td>0</td>
<td>SD-SLR</td>
<td>0.4794</td>
<td>0.4155</td>
<td>0.3617</td>
</tr>
<tr>
<td>1260</td>
<td>0</td>
<td>TSVM</td>
<td>0.3919</td>
<td>0.3382</td>
<td>0.2742</td>
</tr>
<tr>
<td>1260</td>
<td>0</td>
<td>SD-MTJDL-SLR</td>
<td>0.5134</td>
<td>0.4351</td>
<td>0.3845</td>
</tr>
<tr>
<td>0</td>
<td>140</td>
<td>TD-SLR</td>
<td>0.5109</td>
<td>0.4931</td>
<td>0.4031</td>
</tr>
<tr>
<td>0</td>
<td>140</td>
<td>TD-MTJDL-SLR</td>
<td>0.5852</td>
<td>0.5762</td>
<td>0.4918</td>
</tr>
<tr>
<td>1260</td>
<td>140</td>
<td>Merge-SLR</td>
<td>0.5056</td>
<td>0.4541</td>
<td>0.3973</td>
</tr>
<tr>
<td>1260</td>
<td>140</td>
<td>MTJDL-Merge-SLR</td>
<td>0.5196</td>
<td>0.4591</td>
<td>0.3950</td>
</tr>
<tr>
<td>1260</td>
<td>140</td>
<td>MTJDL-MTSLR</td>
<td>0.5975</td>
<td>0.5861</td>
<td>0.5059</td>
</tr>
</tbody>
</table>

The second real HSI data are acquired from the hyperspectral airborne sensor DAIS over the urban areas of Pavia City, Italy\(^1\), in which the Pavia University image is selected as the source scene whose size is 243 × 243 × 72, and the Pavia Center image is selected as the target scene whose size is 400 × 400 × 72. Six common land cover classes are considered for the cross-scene classification, which are listed in Table VI. The data cubes and ground truth maps of both scenes are displayed in Fig. 11. In the experiments on Pavia data, the number of source domain training samples is set to 180 per class, while the number of target domain training samples is set to 20 per class in the case of the training samples in target domain are also available. The classification results of various algorithms are presented in Table VII. The CSMSAD matrix of Pavia data and the confusion matrices produced by different algorithms are shown in Fig. 12. The classification results indicate if the training samples in target scene cannot be obtained, the proposed multitask NMF is an excellent domain adaptation method for cross-scene HSI classification, and if a limited number of the training samples in target scene are available, the combination of MTJDL and MTSLR is an effective technique, i.e., level feature and classifier level domain adaptation should be used together. Another conclusion is that even only very limited number of training samples exist in target scene, they play an important role in the cross-scene classification. Comparing the accuracies of SD-MTJDL-SLR and MTJDL-MTSLR, we can see only a little amount of training samples in target scene (120 per class) bring more than 10% gain in OA, AA, and κ.

Thirdly, we test the proposed methods on Shanghai-Hangzhou scenes. Shanghai and Hangzhou HSI datasets were both captured by EO-1 Hyperion hyperspectral sensor. The Hyperion sensor provides 220 spectral bands, but after removing bad bands, 198 bands remain. Shanghai data set was acquired in Apr. 1st 2002 over Shanghai that is the largest city of China and locates in the east of China. We select an image with the size of 1600 × 230 × 198, which covers some urban and rural areas of Shanghai, including roads, buildings, plants and the water bodies of the Yangtze River and the Huangpu River. Hangzhou data set was captured in Nov. 2nd 2002 over Hangzhou that

\(^1\)We acknowledge Prof. Paolo Gamba in the University of Pavia for providing the DAIS Pavia data.
Fig. 10. CSMSAD matrix and confusion matrices of Indiana data. (a) CSMSAD matrix. (b) confusion matrix of SD-SLR. (c) confusion matrix of TSVM. (d) confusion matrix of SD-MTJDL-SLR. (e) confusion matrix of TD-SLR. (f) confusion matrix of TD-MTJDL-SLR. (g) confusion matrix of Merge-SLR. (h) confusion matrix of Merge-MTJDL-SLR. (i) confusion matrix of MTJDL-MTLSR.

### TABLE VI

**NUMBER OF LABELED SAMPLES IN EACH LAND COVER CLASS WITHIN PAVIA SCENES**

<table>
<thead>
<tr>
<th>Class</th>
<th>Labeled samples</th>
</tr>
</thead>
<tbody>
<tr>
<td>#</td>
<td>Name</td>
</tr>
<tr>
<td>1</td>
<td>Trees</td>
</tr>
<tr>
<td>2</td>
<td>Asphalt</td>
</tr>
<tr>
<td>3</td>
<td>Parking lot</td>
</tr>
<tr>
<td>4</td>
<td>Bitumen</td>
</tr>
<tr>
<td>5</td>
<td>Meadow</td>
</tr>
<tr>
<td>6</td>
<td>Soil</td>
</tr>
</tbody>
</table>
Fig. 11. Source and target scenes in Pavia datasets. The upper one is the source scene (Pavia University), while the lower one is the target scene (Pavia Center). (a) Data cubes. (b) Ground truth maps.

TABLE VII

<table>
<thead>
<tr>
<th>Training sample</th>
<th>Algorithm</th>
<th>OA</th>
<th>AA</th>
<th>(\kappa)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Source Target</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>1080 0</td>
<td>SD-SLR</td>
<td>0.7434</td>
<td>0.7154</td>
<td>0.6752</td>
</tr>
<tr>
<td>1080 0</td>
<td>TSVM</td>
<td>0.6121</td>
<td>0.6150</td>
<td>0.5306</td>
</tr>
<tr>
<td>1080 0</td>
<td>SD-MTJDL-SLR</td>
<td>0.8352</td>
<td>0.8130</td>
<td>0.7906</td>
</tr>
<tr>
<td>0 120</td>
<td>TD-SLR</td>
<td>0.9465</td>
<td>0.9498</td>
<td>0.9323</td>
</tr>
<tr>
<td>0 120</td>
<td>TD-MTJDL-SLR</td>
<td>0.9472</td>
<td>0.9512</td>
<td>0.9331</td>
</tr>
<tr>
<td>1080 120</td>
<td>Merge-SLR</td>
<td>0.8281</td>
<td>0.8137</td>
<td>0.7829</td>
</tr>
<tr>
<td>1080 120</td>
<td>MTJDL-Merge-SLR</td>
<td>0.8428</td>
<td>0.8294</td>
<td>0.8006</td>
</tr>
<tr>
<td>1080 120</td>
<td>MTJDL-MTSLR</td>
<td>0.9507</td>
<td>0.9566</td>
<td>0.9376</td>
</tr>
</tbody>
</table>
Fig. 12. CSMSAD matrix and confusion matrices of Pavia data. (a) CSMSAD matrix. (b) confusion matrix of SD-SLR. (c) confusion matrix of TSVM. (d) confusion matrix of SD-MTJDL-SLR. (e) confusion matrix of TD-SLR. (f) confusion matrix of TD-MTJDL-SLR. (g) confusion matrix of Merge-SLR. (h) confusion matrix of Merge-MTJDL-SLR. (i) confusion matrix of MTJDL-MTSLR.

is the provincial capital of Zhejiang. Hangzhou is also in the east of China, about 170 kilometers far away from Shanghai. A subset with the size of $590 \times 230 \times 198$ is selected from Hangzhou data set. Like the image of Shanghai, Hangzhou image also covers urban and rural areas, including roads, buildings, plants and the water bodies of the West Lake and the Qiantang River. Three land cover classes are labeled for Shanghai and Hangzhou HSIs with the aid of ENVI software. The name of land cover classes and the number of labeled samples are listed in Table VIII. The data cubes and ground truth maps of both scenes are displayed in Fig. 13.

We use Shanghai image as source scene and its number of training samples is set to be 180 per class, while Hangzhou image is used as target scene and the number of target domain training samples is set to 20 per class if available. The experiment results are shown in Table IX and Fig. 14. Different from the results on other data sets, TSVM has a positive effect of improving OA from 0.3264 to 0.8277 in Shanghai-Hangzhou data. However,
Fig. 13. Source and target scenes in Shanghai-Hangzhou datasets. The upper one is the source scene (Shanghai), while the lower one is the target scene (Hangzhou). (a) Data cubes. (b) Ground truth maps.

TABLE VIII
NUMBER OF LABELED SAMPLES IN EACH LAND COVER CLASS WITHIN SHANGHAI-HANGZHOU SCENES

<table>
<thead>
<tr>
<th>Class</th>
<th>Labeled samples</th>
</tr>
</thead>
<tbody>
<tr>
<td>#</td>
<td>Name</td>
</tr>
<tr>
<td>1</td>
<td>Water</td>
</tr>
<tr>
<td>2</td>
<td>Land/Building</td>
</tr>
<tr>
<td>3</td>
<td>Plant</td>
</tr>
</tbody>
</table>

the proposed MTJDL-SLR achieves a higher OA of 0.8933, and the proposed MTJDL-MTSLR has the highest accuracy when the training samples in target scene are available.

Cross-scene classification is important in real applications. From the above experiments, it is concluded that domain adaptation is necessary when labeled samples in source scene are used to help training a classifier for target scene.

Finally, we look back on the concept of SSI that is proposed to measure the degree of spectral shift for
Fig. 14. CSMSAD matrix and confusion matrices of Shanghai-Hangzhou data. (a) CSMSAD matrix. (b) confusion matrix of SD-SLR. (c) confusion matrix of TSVM. (d) confusion matrix of SD-MTJDL-SLR. (e) confusion matrix of TD-SLR. (f) confusion matrix of TD-MTJDL-SLR. (g) confusion matrix of Merge-SLR. (h) confusion matrix of Merge-MTJDL-SLR. (i) confusion matrix of MTJDL-MTSLR.

classification. The SSI values of a synthetic HSI data set and three real HSI data sets are calculated in Table X. The larger the value of SSI, the larger the degree of spectral shift. In other words, the larger the value of SSI, the more necessary of domain adaptation. Shanghai-Hangzhou data set has the largest SSI, so domain adaptation can play a more important role. The classification results support this judgment, because the SRL classifier with dictionary learning based domain adaptation (SD-MTJDL-SLR) increases OA from 0.3264 (obtained by SD-SLR) to 0.8933 when the training samples in target scene are unavailable. Therefore, SSI is a reasonable measurement to estimate spectral shift.
TABLE IX

CLASSIFICATION ACCURACY ON SHANGHAI-HANGZHOU DATA

<table>
<thead>
<tr>
<th>Training sample</th>
<th>Algorithm</th>
<th>OA</th>
<th>AA</th>
<th>k</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Source</td>
<td>Target</td>
<td></td>
<td></td>
</tr>
<tr>
<td>540</td>
<td>SD-SLR</td>
<td>0.3264</td>
<td>0.4465</td>
<td>-0.0240</td>
</tr>
<tr>
<td>540</td>
<td>TSVM</td>
<td>0.8277</td>
<td>0.8678</td>
<td>0.7143</td>
</tr>
<tr>
<td>540</td>
<td>SD-MTJDL-SLR</td>
<td>0.8933</td>
<td>0.9043</td>
<td>0.8167</td>
</tr>
<tr>
<td>0</td>
<td>TD-SLR</td>
<td>0.9142</td>
<td>0.9294</td>
<td>0.8533</td>
</tr>
<tr>
<td>0</td>
<td>TD-MTJDL-SLR</td>
<td>0.9410</td>
<td>0.9566</td>
<td>0.8989</td>
</tr>
<tr>
<td>540</td>
<td>Merge-SLR</td>
<td>0.9200</td>
<td>0.9391</td>
<td>0.8624</td>
</tr>
<tr>
<td>540</td>
<td>Merge-MTJDL-SLR</td>
<td>0.9247</td>
<td>0.9334</td>
<td>0.8680</td>
</tr>
<tr>
<td>540</td>
<td>MTJDL-MTSLR</td>
<td>0.9570</td>
<td>0.9615</td>
<td>0.9250</td>
</tr>
</tbody>
</table>

TABLE X

SSI VALUES OF DIFFERENT DATASETS

<table>
<thead>
<tr>
<th>Dataset</th>
<th>SSI</th>
</tr>
</thead>
<tbody>
<tr>
<td>Synthetic</td>
<td>0.8125</td>
</tr>
<tr>
<td>Indiana</td>
<td>0.7942</td>
</tr>
<tr>
<td>Pavia</td>
<td>0.5359</td>
</tr>
<tr>
<td>Shanghai-Hangzhou</td>
<td>0.8592</td>
</tr>
</tbody>
</table>

V. CONCLUSION

In this paper, we discuss the problem of cross-scene HSI classification. The main challenge of cross-scene classification is spectral shift between different scenes. Multitask NMF based dictionary learning for feature level domain adaptation is proposed to reduce spectral shift by transforming the spectral feature spaces of source and target scenes into a new shared space. Feature level domain adaptation is independent on the specific classifier. Compared with classifier level domain adaptation, it is more flexible and general-purpose. In particular, multitask NMF based dictionary learning has close relation with spectral unmixing under linear spectral mixture model, making its physical interpretation clear. After the new features of samples in source and target scenes are extracted, SLR is chosen as the classifier as it can select a small subset of features with high discriminative power, which can further reduce spectral shift and remedy the shortcoming of unsupervised dictionary learning that no class information is taken into account. Moreover, if a few labeled samples are available in target scene, instead of SLR that trains a single classifier for both source and target scenes, MTSLR is proposed to simultaneously train two classifiers respectively for source and target scene by \( \ell_{2,1} \) norm regularization based joint structure constraint. MTSLR can deal with the residual spectral shift between source and target scenes to improve cross-scene classification performance.

It should be noted that this paper is a preliminary work for cross-scene classification that is a new research problem for HSI in terms of theory and application. A lot of approaches derived from domain adaptation and transfer learning can be studied to make them suitable for cross-scene HSI classification. One future work is to study other multitask dictionary learning techniques, especially when the dictionary not only has the task-related
common atoms reflecting cross-scene correlation, but also atoms involving individual characteristics. Another work is to extend cross-scene classification to different remote sensing sensors, i.e., source and target scene images captured from different imaging sensors, by combining information fusion and domain adaptation techniques.

REFERENCES


